

Part XI

Conclusions

Concluding Perspective

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Abstract. This meeting has covered a broad agenda. This contribution to the concluding session offers comments on some current controversies, and on the prospects for cosmology in the coming decade.

1. Preamble

The last two years have been memorable for cosmologists. The key parameters defining our universe's gross properties – hitherto tentative and uncertain – have seemingly been pinned down more narrowly. Moreover, the favoured values are concordant with a specific consistent model (though in some ways an unexpected one). To put this rapid advance in perspective, we should remind ourselves of how the cosmological discourse has evolved during the eight decades since astronomers became aware of the extragalactic cosmos.

Models for homogeneous isotropic universes date from the 1920s and 1930s, and evidence for an expanding universe from the 1920s; but not until the 1950s was there any prospect of discriminating among the various models. Indeed, there was even then little quantitative data on how closely any isotropic homogeneous model fitted the actual universe.

A cosmology meeting in the 1950s would have focussed on the question: is there evidence for evolution, or is the universe in a steady state? Key protagonists on the theoretical side would have included Bondi, Gold and Hoyle. Ryle would have been arguing that counts of radio sources – objects so powerful that many lay beyond the range of optical telescopes – already offered evidence for cosmic evolution; and Sandage would have advocated the potential of the Mount Palomar 200 inch telescope for extending the Hubble diagram far enough to probe the deceleration. Intimations from radio counts that the universe was indeed evolving were strengthened after 1963 by the redshift data on quasars.

The era of physical cosmology of course began in 1965, when the discovery of the microwave background brought the early 'fireball phase' into the realm of empirical science, and the basic physics of the 'hot big bang' was worked out. (The far earlier contributions by Gamow's associates, Alpher and Herman, continued, however, to be under-appreciated). There was also substantial theoretical work on anisotropic models, etc. Throughout the 1970s this evidence for the 'hot big bang' firmed up, as did the data on light elements, and their interpretation as primordial relics.

Theoretical advances in the 1980s gave momentum to the study of the ultra-early universe, and fostered the 'particle physics connection': the sociolog-

ical mix of cosmologists changed. There was intense discussion of inflationary models, non-baryonic matter, and so forth.

Within the last decade, the pace has been accelerating. This is because of a confluence of developments.

1. *The microwave background fluctuations*: these were first detected by COBE in 1992, and are now being probed with enough sensitivity, and on a sufficient range of angular scales, to provide crucial tests of inflation and to discriminate among different models. Ground-based and balloon experiments will next year be supplemented by the all-sky coverage of the MAP satellite.

2. *The high-redshift universe*: the Hubble Space Telescope (HST) has fulfilled its potential; two Keck Telescopes have now been joined by the VLT, Subaru, and Gemini. We're used to quasars at very high redshifts. But quasars are rare and atypical – we'd really like to know the history of matter in general. One of the most important recent advances has been the detection of many hundreds of galaxies at redshifts up to (and even beyond) 5. Absorption due to the hundreds of clouds along the line of sight to quasars probes the history of cosmic gas in exquisite detail. These have opened up the study of 'ordinary' galaxies right back to large redshifts, and to epochs when they were newly formed. And two recently-launched new X-ray telescopes, Chandra and XMM/Newton, will offer higher resolution and higher sensitivity for the study of distant galaxies and clusters.

3. *Large scale clustering and dynamics*. Large-scale surveys such as the 2dF and the SDSS are vastly enhancing quantitative data on galaxies and the statistics of their clustering. Simultaneously with this progress, there have been dramatic advances in computer simulations. These now incorporate realistic gas dynamics as well as gravity.

4. *Developments in fundamental physics* are offering new speculative insights, which figure prominently in the ongoing debates about the ultra-early universe.

2. The Cosmological Numbers

Traditionally, cosmology was the quest for a few numbers. The first were H , q , and Λ . Since 1965 we've had another: the baryon/photon ratio. This is believed to result from a small favouritism for matter over antimatter in the early universe – something that was addressed in the context of 'grand unified theories' in the 1970s. (Indeed, baryon non-conservation seems a prerequisite for any plausible inflationary model. Our entire observable universe, containing at least 10^{79} baryons, could not have inflated from something microscopic if baryon numbers were strictly conserved.)

In the 1980s non baryonic matter became almost a natural expectation, and Ω_b/Ω_{DM} is another fundamental number.

Another specially important dimensionless number tells us how smooth the universe is. It's measured by

- The Sachs-Wolfe fluctuations in the microwave background effects
- the gravitational binding energy of clusters as a fraction of their rest mass

- or by the square of the typical scale of mass- clustering as a fraction of the Hubble scale.

It's of course oversimplified to represent this by a single number Q , but insofar as one can, its value is pinned down to be 10^{-5} . (Detailed discussions introduce further numbers: the ratio of scalar and tensor amplitudes, and quantities such as the 'tilt', which measure the deviation from a pure scale-independent Harrison-Zeldovich spectrum.)

What's crucial is that Q is small. Numbers like Ω and H are only well-defined insofar as the universe possesses 'broad brush' homogeneity – so that our observational horizon encompasses many independent patches each big enough to be a fair sample. This wouldn't be so, and the simple Friedmann models wouldn't be useful approximations, if Q weren't much less than unity. Its smallness is necessary if the universe is to look homogeneous. But it isn't, strictly speaking, sufficient – a luminous tracer that didn't weigh much could be correlated on much larger scales without perturbing the metric. Simple fractal models for the luminous matter are however ruled out by other observational constraints, such as the isotropy of the X-ray background, and of the radio sources detected in deep surveys.

3. How Firmly-Based are Current Models?

After the first millisecond – after the quark-hadron transition – conditions are so firmly within the realm of laboratory tests that there are no crucial uncertainties in the microphysics (though we should leave our minds at least ajar to the possibility that some 'constants' may actually be time-dependent). And according to the standard model everything is then fairly uniform – perturbations are still in the linear regime.

It's easy to make quantitative predictions that pertain to this intermediate era, stretching from a millisecond to a million years. And we've now got high-quality data to confront them with. The marvellous COBE 'black body' pins down the microwave background spectrum to a part in 10,000. The theoretical framework for light element nucleosynthesis goes back more than 30 years, but the debate (concurrence or crisis?) now focuses on 1 per cent effects in helium spectroscopy, and on traces of deuterium at very high redshifts. The case for extrapolating back to a millisecond is compelling and battle-tested. Insofar as there's a 'standard model' in cosmology, this is now surely part of it.

When the primordial plasma recombined, after half a million years, the black body radiation shifted into the infrared, and the universe entered, literally, a dark age. This lasted until the first stars lit it up again. The basic microphysics remains, of course, straightforward. But once non-linearities develop and bound systems form, gravity, gas dynamics, and the physics in every volume of Landau and Lifshitz combine to unfold the complexities we see around us and are part of. The later universe, after the dark age is over, is messy and complex – difficult for the same reason that all environmental sciences are difficult.

A decade from now, when the Next Generation Space Telescope (NGST) flies, we may know the main cosmological parameters, and have exact simulations of how the dark matter clusters. But reliable knowledge of how stars form, when the intergalactic gas is reheated, and how bright the first 'pregalaxies'

are will still involve parameter-fitting, guided by observations. The aim is get a consistent model that not only matches all we know about galaxies at the present epoch, but also the increasingly detailed snapshots of what they looked like, and how they were clustered, at all earlier times.

But don't be too gloomy about the messiness of the 'recent' universe. There are some 'cleaner' tests. Simulations can reliably predict the present clustering and large-scale distribution of non-dissipative dark matter. This can be observationally probed by weak lensing, large scale streaming, and so forth, and checked for consistency with the CMB fluctuations, which probe the linear precursors of these structures.

4. Dark Matter: What, and How Much?

The nature of the dark matter – how much there is and what it is – still eludes us. It's embarrassing that 90 percent of the universe remains unaccounted for.

This key question may yield to a three-pronged attack:

1. *Direct detection.* Astronomical searches for 'machos' in the Galactic Halo have shown that only a minority of the halo dark matter could be in this form. Indeed nucleosynthesis arguments (especially the D abundance) strongly suggest that most dark matter is non-baryonic. Several groups are developing cryogenic detectors to search for supersymmetric particles and axions.

2. *Progress in particle physics.* Important recent measurements suggest that neutrinos have non-zero masses; this result has crucially important implications for physics beyond the standard model. However the inferred masses seem too low to be cosmologically important. If theorists could pin down the properties of supersymmetric particles, the number that survive from the big bang could be calculated just as we now calculate the helium and deuterium made in the first three minutes. Optimists may hope for progress on still more exotic options.

3. *Simulations of galaxy formation and large-scale structure.* When and how galaxies form, the way they are clustered, and the density profiles within individual systems, depend on what their gravitationally-dominant constituent is, and simulations are now constraining the options, and revealing possibly-severe problems with 'standard' collisionless cold dark matter.

5. New Standard Model

Several lines of evidence suggest that the gravitating dark matter (which is predominantly non-baryonic) contributes substantially less than $\Omega_{DM} = 1$.

(i) The baryon fraction in clusters is 0.15 – 0.2. On the other hand, the baryon contribution to Ω is now pinned down by deuterium measurements to be around $0.015 h^2$. If clusters are a fair sample of the universe, then this is incompatible with a dark matter density high enough to make $\Omega_{DM} = 1$.

(ii) The presence of clusters of galaxies with $z = 1$ is hard to reconcile with the rapid recent growth of structure that would be expected if Ω_{DM} were unity.

(iii) The Supernova Hubble diagram (even though the case for actual acceleration may not be compelling) seems hard to reconcile with the large deceleration implied by an Einstein-de Sitter model.

(iv) The inferred ages of the oldest stars are only barely consistent with an Einstein-de Sitter model, for the favoured choices of Hubble constant.

If there were no evidence other than (i)-(iv) above, then an open model with $0.2 - 0.3$ would be tenable. But perhaps the most important development during the last year has been the strengthening evidence that the angular scale of the ‘doppler peaks’ in the CMB angular fluctuations favours a flat universe – gratifying to theorists. But it is a model where baryons make up 4 percent, dark matter about 25 percent, and vacuum energy (or some non-clustered negative-pressure component that accelerates cosmic expansion) makes up the balance.

The universe is more complicated than some people hoped. Is it contrived that the vacuum-energy should have the specific small value that leads it to start dominating just at the present epoch?

6. A History of Lambda

Λ was of course introduced by Einstein in 1917 to permit a static unbounded universe. After 1929, the cosmic expansion rendered Einstein’s motivation irrelevant. However, by that time de Sitter had already proposed his expanding Λ -dominated model. In the 1930s, Eddington and Lemaitre proposed that the universe had expanded (under the action of the Λ -related repulsion) from an initial Einstein state. Λ fell from favour after the 1930s: relativists disliked it as a field ‘acting on everything but acted on by nothing’. A brief resurgence in the late 1960s was triggered by a (now discredited) claim for a pile-up in the redshifts of quasars at a value of z slightly below 2. The CMB had already convinced most people that the universe emerged from a dense state, rather than from an Einstein static model, but it could have gone through a coasting or loitering phase where the expansion almost halted. A large range of affine distance would then correspond to a small range of redshifts, thereby accounting for a ‘pile up’ at a particular redshift. It was also noted that this model offered more opportunity for small-amplitude perturbations to grow.

The ‘modern’ interest in Λ stems from its interpretation as a vacuum energy. The interest has of course been hugely boosted recently, through the claims that the Hubble diagram for Type 1A supernovae indicates an acceleration. This leads to the reverse problem: Why is Λ about 120 powers of 10 smaller than its ‘natural’ value, even though the effective vacuum density must have been very high in order to drive inflation? One solution to this dilemma is to postulate a new field (‘quintessence’) which has, like vacuum energy, a negative pressure but can decay during cosmic expansion. As has been described at this meeting, it is in principle possible to distinguish this option from a ‘traditional’ time-independent Λ .

(If Λ is fully resurrected, it will be a great ‘coup’ for de Sitter. His model, dating from the 1920s, not only describes inflation, but would also describe future aeons of our cosmos with increasing accuracy. Only for the 50–odd decades of logarithmic time between the end of inflation and the present would it need modification!).

7. Inflation and the Very Early Universe

7.1. Testing specific inflation models

The gross properties of our universe, and indeed its overall scale, are determined by physics as surely as the He and D abundances – it's just that the conditions at the ultra-early eras when the baryon and dark matter densities, and Q , were fixed are far beyond anything we can experiment on.

The inflation concept is the most important single idea. It suggests why the universe is so large and uniform – indeed, it suggests why it is expanding. It was compellingly attractive when first proposed, and most cosmologists (with a few eminent exceptions like Roger Penrose) would bet that it is, in some form, part of the grand cosmic scheme.

Inflationary models still cannot 'naturally' account for the fluctuation amplitude $Q = 10^{-5}$. It's important to be clear about the methodology and scientific status of such discussion. I comment with great diffidence, because I'm not an expert here.

The physics of the ultra-early universe remains conjectural, but one can constrain it by testing particular variants of inflation. For instance, definite assumptions about the physics of the inflationary era have calculable consequences for the fluctuations – whether they're gaussian, the ratio of scalar and tensor modes, the tilt, and so forth – which can be probed by observing large scale structure and, even better, by microwave background observations. Measurements with the MAP and Planck/Surveyor spacecraft will surely tell us things about 'grand unified' physics that can't be directly inferred from ordinary-energy experiments.

7.2. A multiverse: is the concept genuinely a scientific hypothesis?

Some theories about 'extreme physics', when applied to the ultra-early universe, yield many universes that sprout from separate big bangs into disjoint regions of space-time. But we do not yet have good reason to trust such theories. However, if superstrings (or some other equally comprehensive theory) were 'battle tested' by convincingly explained things we could observe, then if it predicts multiple universes we should take them seriously too, just as we give credence to what our current theories predict about quarks inside atoms, or the regions shrouded inside black holes.

The 'multiverse' is, of course, a highly speculative concept. However, the question 'Do other 'universes' exist?' is one for scientists – it isn't just metaphysics. The following chain of reasoning may not be absolutely compelling, but should at least erase any prejudice that the concept is absurd.

We can envisage a succession of 'horizons', each taking us further than the last from our direct experience:

(i) *Galaxies beyond range of present-day telescopes.* There is a limit to how deep in space, and how far back in time, our present-day instruments can probe. Obviously there is nothing fundamental about this limit – it is constrained just by technology, and enlarges from year to year. We would not demote very distant galaxies from the realm of science simply because they haven't been seen yet – many more will undoubtedly be revealed in the coming decades by projected telescope arrays in space.

(ii) *Galaxies unobservable – even in principle – until a remote cosmic future* Even if there were absolutely no technical constraints on the power of telescopes, our observations are still bounded by the ‘particle horizon’. This horizon demarcates the ‘shell’ around us on which the redshift would be infinite. There is nothing special about the galaxies on this horizon, any more than there is anything special about the circle that defines the horizon when you’re in the middle of an ocean. On the ocean, you can see further by climbing up your ship’s mast. But our cosmic horizon can’t be extended unless the universe changes, so as to allow light to reach us from galaxies that are now beyond it.

If the expansion were decelerating, then the far-future ‘horizon’ would encompass some galaxies that are now undetectable even in principle. The ‘horizon’ only grows perceptibly over the aeons of cosmic evolution. It is, to be sure, a practical impediment if we have to await a cosmic change taking billions of years, rather than just a few decades (maybe) of technical advance, before a prediction can be put to the test. But does that introduce a difference of principle? Surely it is still meaningful to talk about these faraway galaxies, and the far longer time before they can be observed is a merely quantitative difference, not one that changes their epistemological status?

(iii) *Galaxies that emerged from ‘our’ big bang, but are unobservable in principle, ever.* But what about galaxies that we can never see, however long we wait? These are a feature of (for instance) Λ -dominated cosmological models where the expansion accelerates. There would (as in a decelerating universe) be galaxies so far away that no signals from them have yet reached us. But if the cosmic repulsion has overwhelmed gravity, we are now accelerating away from them, so if their light hasn’t yet reached us, it never will. Such galaxies wouldn’t become observable however long we waited. But does that make them less ‘real’ than they would be if they were destined to become observable a trillion years hence?

(iv) *Galaxies in disjoint universes* The never-observable galaxies in (iii) would have emerged from the same homogeneous ‘big bang’ as us. But suppose that, instead of causally-disjoint regions emerging from a single big bang (via an episode of inflation) we envisage separate big bangs. Are space-times completely disjoint from ours any less real than parts of what we’d traditionally call our own universe that never come within our horizon?

This four-step argument (some may call it a ‘slippery slope’) tells us, I think, that other universes, even if they are never observable, are within the remit of science.

If there are other universes, one question that arises is: How much variety might they display? Which features of our actual universe are contingent rather than necessary? Many would agree with Wilczek that the most important question in 21st century physics is: ‘Are the laws of physics unique?’ A ‘final theory’ might determine uniquely particle masses and coupling constants, and even numbers like Q and the curvature. There would then be no role for ‘anthropic’ arguments in cosmology. On the other hand, the (still unknown) underlying laws that apply throughout the multiverse could turn out to be more permissive. Each universe may then expand in a distinctive way. Some of its key properties may then be ‘accidents’, and there would be no explanation for them other than an anthropic one.

7.3. Bayesian tests of whether our universe is drawn from a specific type of ensemble

Suppose that the basic numbers describing our universe are an arbitrary outcome of how it cooled down, and take different values in other universes. Their values in our universe may not be typical of the entire multiverse: our universe must have been special, and probably highly atypical, to permit our existence. But we would need to think again if the numbers turned out to be *even more special* than our presence requires. Even in our present ignorance of fundamental theory, we can use a Bayesian argument to test specific hypotheses.

Consider Λ . An unduly fierce cosmic repulsion would prevent galaxies from forming. It has to be below a readily calculable threshold to allow protogalaxies to pull themselves together before gravity is overwhelmed by cosmical repulsion. But we wouldn't expect it to be too far below that threshold. Suppose, for instance, that (contrary to current indications) Λ was thousands of times smaller than it needed to be merely to ensure that galaxy formation wasn't prevented. This would raise suspicions that it was indeed zero for some fundamental reason. (Or that it had a discrete set of possible values, and all the others were well about the threshold). By this line of argument we could in principle find strong evidence against specific hypothesis about a multiverse: the parameters of our universe should not be too atypical of the anthropically-allowed subset of universes in the ensemble, weighted by the (theory-generated) prior probability distribution.

7.4. A historical parallel

The multiverse concept might seem arcane, even by cosmological standards, but it affects how we weigh the observational evidence in some current debates. Our universe doesn't seem to be quite as simple as it might have been. It contains atoms, and dark matter; as an extra complication, there is some kind of 'dark energy' in empty space. Some theorists have a strong prior preference for the simplest universe and are upset by these developments. It now looks as though a craving for such simplicity will be disappointed.

Perhaps we can draw a parallel with debates that occurred 400 years ago. Kepler discovered that planets moved in ellipses, not circles. Galileo was upset by this. He thought circles seemed more beautiful; and they were simpler – one parameter not two. Newton later showed, however, that all elliptical orbits could be understood by a single unified theory of gravity. Had Galileo still been alive when 'Principia' was published, Newton's insight would surely have joyfully reconciled him to ellipses.

The parallel is obvious. A universe with low Ω_{DM} , non-zero Λ , and so forth may seem ugly and complicated. But maybe this is our limited vision. Our Earth traces out just one ellipse out of an infinity of possibilities, its orbit being constrained only by the requirement that it allows an environment conducive for evolution (not getting too close to the Sun, nor too far away). Likewise, our universe may be just one of an ensemble of all possible universes, constrained only by the requirement that it allows our emergence. Maybe we should go easy with Occam's razor and be wary of arguments that $\Omega = 1$ and $\Lambda = 0$ are *a priori* more natural and less ad hoc.

8. The Agenda 10 Years From Now: A Bifurcated Community?

If we were to reconvene 10 years from now, what would be the ‘hot topics’ on the agenda? The key numbers specifying our universe and its content may by then have been pinned down. Or we may discover that our universe is too complicated to fit into the framework. I’ve heard people claim that cosmology will thereafter be less interesting – that the most important issues will be settled, leaving only the secondary drudgery of clearing up some details. I’d like to spend a moment trying to counter that view.

It may turn out, of course, that the new data don’t fit anywhere within the parameter-space that these numbers are derived from. (I was tempted to describe this as ‘pessimistic’, but of course some people may prefer to live in a more complicated and challenging universe!) On the other hand, maybe everything will fit the framework, and we will pin down the contributions to Ω from baryons, CDM, dark energy, and the vacuum, along with the amplitude and tilt of the fluctuations, and so forth. If that happens, it will signal a great triumph for cosmology – we will know the ‘measure of our universe’ just as, over the last few centuries, we’ve learnt the size and shape of our Earth and Sun.

Our focus will then be redirected towards new challenges, as great as the earlier ones. But the character and ‘sociology’ of our subject will change: it will bifurcate into two sub-disciplines. In sociological terms, this bifurcation would be analogous to what actually happened in the field of general relativity 20-30 years ago. The ‘heroic age’ of general relativity – leading to the rigorous understanding of gravitational waves, black holes, and singularities – occurred in the 1960s and early 1970s. Thereafter, the number of active researchers in ‘classical’ relativity declined (except maybe in computational aspects of the subject): most of the leading researchers shifted either towards astrophysically-motivated problems, or towards quantum gravity and ‘fundamental’ physics.

What will be the foci of the two branches of cosmology we’ll be pursuing a decade from now? One will be ‘environmental cosmology’ – understanding the emergence of structure, stars and galaxies. The other will focus on the fundamental physics of the ultra-early universe (pre-inflation, m-branes, multiverses, etc). A few words about each of these:

Environmental cosmology: long range prospects One continuing challenge will be to explore the emergence of structure. This is a tractable problem until the first star (or other collapsed system) forms. But the huge dynamic range and uncertain feedback thereafter renders the phenomena too complex for any feasible simulation. Even if the clustering of the CDM under gravity could be exactly modelled, along with the gas dynamics, then as soon as the first stars form we face major uncertainties that will still be a challenge to the petaflop simulations being carried out a decade from now. We will still need the NGST to pin down what happened in the earliest stages of galaxy formation.

Probing the Planck era and ‘beyond’ The second challenge would be to firm up the physics of the ultra-early universe. Perhaps the most ‘modest’ expectation would be a better understanding of the candidate dark matter particles: if the masses and cross-sections of supersymmetric particles were known, it should be possible to predict how many survive, and their contribution to Ω , with the

same confidence as that with which we can compute primordial nucleosynthesis. Associated with such progress, we might expect a better understanding of how the baryon-antibaryon asymmetry arose, and the consequence for Ω_b .

A somewhat more ambitious goal would be to pin down the physics of inflation. Knowing parameters like Q , the tilt, and the scalar/tensor ratio will narrow down the range of options. The hope must be to make this physics as well established as the physics that prevails after the first millisecond.

Better still, new insights and unifications will tell us whether or not that are new scales of complexity far beyond our present horizon.

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