

New self-consistent wind parameters to fit optical spectra of O-type stars

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Abstract. We perform spectral fittings for O-type stars based on self-consistent wind solutions, providing \dot{M} and $v(r)$ directly derived from the initial stellar parameters. We introduce our two methods: m-CAK prescription and Lambert-procedure.

The Lambert-procedure allows the calculation of consistent $v(r)$ that reduce the number of free parameters when a spectral fitting using CMFGEN is performed, even without recalculation of the \dot{M} . Spectra calculated from our Lambert-solutions show significant differences compared to the initial β -law CMFGEN models. For m-CAK prescription, self-consistent solutions provide values for theoretical \dot{M} on the order of the most recent predictions from other studies. Later, we find a global fit with the RT code FASTWIND. This is an important step towards the determination of stellar and wind parameters without using β -law. Our m-CAK prescription is valid for the O-type stars with $T_{\text{eff}} \geq 30$ kK and $\log g \geq 3.2$.

We expect that solutions introduced here to be extended to numerous studies about massive stars in future.

Keywords. Early-type stars, Hydrodynamics, Stellar winds

1. The Lambert-procedure

Given the radiative acceleration $g_{\text{rad}}(r)$ calculated by CMFGEN, we have the wind equation of motion

$$v \frac{dv}{dr} = -\frac{1}{\rho} \frac{dp}{dr} - \frac{GM_*}{r^2} + g_{\text{rad}}(r), \quad (1)$$

new velocity profile $v(r)$ is analytically calculated

$$\Rightarrow -\hat{v}^2 e^{-\hat{v}^2} = -\left(\frac{\hat{r}_c}{\hat{r}}\right)^4 \exp\left[-1 - 2\hat{v}_{\text{crit}}^2 \left(\frac{1}{\hat{r}} - \frac{1}{\hat{r}_c}\right) - 2 \int_{\hat{r}_c}^{\hat{r}} \hat{g}_{\text{line}} d\hat{r}\right] \quad (2)$$

by implementing the Lambert W -function as

$$\hat{v}(\hat{r}) = \sqrt{-W(x(\hat{r}))}. \quad (3)$$

This is iteratively implemented, until convergence is achieved. Mass-loss rate \dot{M} is a free parameter for the Lambert-procedure, but it needs to be constrained to accurately satisfy the full equation of motion in CMFGEN, including clumping.

$$\left(v - \frac{a^2}{v}\right) \frac{dv}{dr} = g_{\text{rad}} - \frac{GM_*}{r^2} + 2\frac{a^2}{r} + \frac{a^2}{f} \frac{df}{dr}. \quad (4)$$

Results of this procedure are shown in Table 1.

Table 1. Results for our modelled stars using the Lambert-procedure (Gormaz-Matamala et al. 2021)

	ζ -Puppis	HD 163758	α -Cam
T_{eff} [kK]	41	34.5	28.2
$\log g$	3.6	3.4	2.975
R_*/R_\odot	17.9	19.1	30.3
v_∞ [km s ⁻¹]	2740	2400	2650
\dot{M} [$10^{-6}M_\odot$ yr ⁻¹]	2.7	1.2	0.85
f_∞ [$1/D_\infty$]	0.10	0.05	0.05

Table 2. Stellar and wind parameters for HD 192639, obtained using the m-CAK prescription (Gormaz-Matamala et al. 2022a)

HD 192639			
T_{eff} (kK)	34.0	$(k, \alpha, \delta)_{\text{sc}}$	(0.047, 0.694, 0.089)
$\log g$	3.25	$\log \dot{M}_{\text{sc}}$ (M_\odot yr ⁻¹)	-5.783 ± 0.90
R_*/R_\odot	19.8	v_∞ (km s ⁻¹)	1460 ± 160
M_*/M_\odot	25.4	f_{cl}	6.25
L_*/L_\odot	4.73×10^5	v_{rot} (km s ⁻¹)	100
[He/H]	0.10	$\log D_{\text{mom}}$	28.83

2. The m-CAK prescription

Equation of motion is solved using the line-force parameters k , α and δ (Gormaz-Matamala et al. 2019)

$$v \frac{dv}{dr} = -\frac{1}{\rho} \frac{dp}{dr} - \frac{GM_{\text{eff}}}{r^2} + g_{\text{es}}(r) k t^{-\alpha} \left(\frac{N_e}{W}\right)^\delta. \tag{5}$$

Line-force parameters (k, α, δ) are self-consistently calculated with the wind hydrodynamics, by means of the force-multiplier ($\mathcal{M}(t)$) which is defined as a function of the independent optical depth (t)

$$\mathcal{M}(t) = k t^{-\alpha} \left(\frac{N_e}{W}\right)^\delta = \frac{g_{\text{line}}}{g_{\text{es}}}, \text{ with } t = \sigma_{\text{es}} v_{\text{th}} \rho(r) \left(\frac{dv}{dr}\right)^{-1}, \tag{6}$$

We generate a large grid with of solutions for the line-force parameters, for different values of effective temperatures and surface gravities. Self-consistent solution is delimited to a specific range of t , which depends on the hydrodynamic conditions such as incorporation of temperature structure $T(r)$. New self-consistent values for mass-loss rate (\dot{M}_{sc}) and terminal velocity ($v_{\infty, \text{sc}}$) are obtained, which are used to perform synthetic spectra and determine new stellar and wind parameters. Results for the star HD 192639 are shown in Table 2.

Because wind parameters \dot{M}_{sc} and $v_{\infty, \text{sc}}$ now depend on stellar parameters, we do our spectral fittings reducing the number of free parameters. Mass-loss rates derived from the m-CAK prescription can be applied for the generation of evolutionary tracks for massive stars (Gormaz-Matamala et al. 2022b, accepted in A&A).

References

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