# DIELECTRIC-RELAXATION SPECTROSCOPY OF KAOLINITE, MONTMORILLONITE, ALLOPHANE, AND IMOGOLITE UNDER MOIST CONDITIONS

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Abstract—The dielectric behavior of kaolinite, montmorillonite, allophane, and imogolite samples adjusted to a water potential of 33 kPa was examined using a time-domain reflectometry method over a wide frequency range of  $10^3$ – $10^{10}$  Hz. A dielectric relaxation peak owing to bound H<sub>2</sub>O was observed. The observation of this peak required the precise determination of the contributions of dc conductivity. The peak is located at 10 MHz, indicating that the relaxation time of the bound H<sub>2</sub>O is approximately ten times longer than the relaxation time of bound H<sub>2</sub>O with organic polymers, such as an aqueous globular-protein solution. The structure of bound H<sub>2</sub>O differs between phyllosilicates and amorphous phases, based on differences in relaxation strength and the pattern of distribution of the relaxation times. The dielectric process involving rotation of bulk H<sub>2</sub>O molecules was also observed at 20 GHz. The relaxation strength of bulk H<sub>2</sub>O increased with an increase in the water content. The interfacial polarization in the diffuse double layer occurred only in montmorillonite and kaolinite, indicating that mechanisms involving the Maxwell-Wagner and surface-polarization effects cannot be extended to include allophane and imogolite. Although these results suggest that additional work is required, a tentative conclusion is that a tangential migration of counter-ions along clay surfaces may be important.

Key Words—Allophane, Bound Water, Complex Permittivity, Dielectric-Relaxation Spectroscopy, Imogolite, Interfacial Polarization, Kaolinite, Montmorillonite, Time-Domain Reflectometry.

## INTRODUCTION

Dielectric-relaxation spectroscopy probes a molecular environment on the broad time domain between  $10^{-12}-10^{-2}$  s, compared with other methods, such as nuclear magnetic resonance (NMR) spectroscopy whose time scale is between  $10^{-10}-10^{-3}$  s. Therefore, dielectric-relaxation spectroscopy provides data concerning many molecular arrangements of H<sub>2</sub>O depending on the time scale involved (Sposito and Prost, 1982). In clay-mineral studies, dielectric measurements obtain information about the bound H<sub>2</sub>O on clay surfaces (*e.g.*, Fripiat *et al.*, 1965; Mamy, 1968; Weiler and Chaussidon, 1968; Hoekstra and Doyle, 1971; Calvet, 1975; Hall and Rose, 1978) and about the interfacial region between clay particles (*e.g.*, Lockhart, 1980a, 1980b; Raythatha and Sen, 1986).

Mamy (1968) and Calvet (1975) performed dielectric measurements on one-layer hydrated montmorillonite by changing the temperature at a fixed frequency between 300 Hz and 10 kHz. They concluded that the rotational motions of bound H<sub>2</sub>O on Na- and Krich montmorillonite are on the same scale as those in free H<sub>2</sub>O. On the other hand, the rotational times on the montmorillonite saturated with bivalent cations are comparable to ice (Sposito and Prost, 1982). The conclusion implies that the relaxation times of bound H<sub>2</sub>O are separated by  $\sim 10^5$  orders of magnitude, depending on the solvation complexes formed with the exchangeable cations. For an aqueous electrolyte solution, NMR data indicate that the rotational correlation times for  $H_2O$  molecules in the first hydration sphere around the cation might be different by no more than one order in magnitude between monovalent and bivalent cations (Hertz, 1973). In general, for isotropic motion, the NMR correlation time is more closely related to the dielectric-relaxation time because the latter is three times the former (*e.g.*, Carrington and McLachlan, 1967). Furthermore, the relation is applicable to the correlation time and the relaxation time for bound  $H_2O$  in biopolymer solutions (Fukuzaki *et al.*, 1992, 1995). The large difference in the dielectric-relaxation time probably cannot be explained by only the small difference owing to the solvation of exchangeable cations.

Hall and Rose (1978) measured dielectric-absorption curves for kaolinite at very low-water contents over the frequency range of 100 to 10 MHz. One absorption peak was found. The mechanism responsible for absorption was concluded to be caused by  $H_2O$ molecules bound to kaolinite. Judging from the values of the relaxation time,  $H_2O$  molecules in a one-layer hydrate have strong similarities to an "ice-like structure", the exchangeable cation is monovalent. These results are not consistent with those for montmorillonite (see above). Note, however, that there is evidence of another absorption found at near 10 MHz.

Lockhart (1980a, 1980b) obtained dielectric-dispersion curves for montmorillonite and kaolinite suspensions over the frequency range similar to that used by Hall and Rose. The suspensions varied between highly dilute to thick. Only one relaxation process was attributed to polarization of the surface double layer. Because these results were not obtained at a high resolution of frequency, the relaxation process owing to bound  $H_2O$  could not be identified, even if the relaxation existed. Thus, bound  $H_2O$  on clay suspensions or moist clays was thought to be difficult to ascertain, because the solvent usually has a large dielectric constant and the relaxation strength of bound  $H_2O$  is thought too small to be observed.

Most of the previous results were obtained by measuring a narrow frequency range, especially low frequencies, or by changing the temperature at a fixed frequency. Therefore, these experimental conditions may limit the resulting conclusions. Previous results suggest that clay-water systems have multiple relaxation processes, such as interfacial polarizations around the clay particles and rotational relaxation of bound and free H<sub>2</sub>O; therefore, the dielectric behavior is expected to be complicated. Useful and precise dielectric information may be obtained only when each relaxation process is extracted from the complicated overall behavior based on the measurement over wide frequency ranges and at high resolutions. Another problem is that the dielectric results from previous studies are restricted to very low-water contents. Because the physicochemical states of H<sub>2</sub>O and counter-ions near the clay surfaces change with increasing water content, the dielectric results obtained at a low-water content may not be applicable to other water contents. Ishida and Makino (1999a, 1999b) showed that the dielectric properties of clay suspensions are different from those at very low-water contents. However, dielectric properties under moist conditions are not yet clarified.

Time-domain reflectometry (TDR) employed in the present study gives the complex permittivity continuously over a wide frequency domain (1 kHz to 20 GHz); therefore, it is easy to extract each relaxation process. In general, clay-water systems under moist conditions have a high dc conductivity. Hence, the contribution of dc conductivity to the complex permittivity must be precisely evaluated, especially in the low-frequency range. This evaluation is possible using a reference TDR method (Cole et al., 1980; Mashimo et al., 1987a). If a standard sample with known permittivity is employed as a reference and the conductivity is adjusted to be approximately the same as that of an unknown sample, the complex permittivity of the unknown sample can be obtained as a function of the ratio of the Fourier transforms of the two reflected waves from the known and the unknown samples, respectively.

In this study, the TDR method was used to investigate the dielectric properties of moist minerals. Our focus is on ascertaining the relaxation parameters of bound  $H_2O$ , especially the relaxation time. By using this method, bound  $H_2O$  was confirmed in biopolymers, such as DNA (Mashimo *et al.*, 1989), globular protein (Miura *et al.*, 1994), aqueous solutions, and moist collagen (Shinyashiki *et al.*, 1990). For moist collagen, the relaxation strength observed at 100 MHz depends on the water content and does not occur for dried collagen. Thus, this process is caused by the orientation of strongly bound H<sub>2</sub>O to topocollagen. The relaxation strength at 100 MHz for the globular proteins is in proportion to the surface area of these proteins, suggesting that the relaxation process is caused by the orientation of bound H<sub>2</sub>O molecules on the protein surface.

Our interest also relates to the mechanism responsible for a very large low-frequency relaxation process. Possible mechanisms include the Maxwell-Wagner effect and the surface-polarization effect. The former occurs in material composed of a layer of insulating material covered with a layer of conduction medium. Clay samples can be regarded as mixtures of a conduction medium (the water in all the different forms) and an insulating material (silicate layer of the clay mineral). The latter is ascribed to the net displacement of counter-ions as a result of the influence of an external electric field and hence is caused by deformation of the diffuse lining of the double layer. In deducing the boundary conditions of the Maxwell-Wagner polarization theory, the tangential flux of electrical charges is considered negligible in comparison with the normal flux because the space charge is very thin near the surface of the insulating material. However, the surface-polarization theory includes the tangential flux. The Maxwell-Wagner theory may not be correct if the particle surface carries a sufficiently high charge that the concentration of the counter-ions, and thus the conductivity in the diffuse part of the double layer, substantially exceeds the conductivity in the bulk (Dukhin, 1973).

Samples for study were kaolinite, montmorillonite, allophane, and imogolite. As far as we know, moist allophane and imogolite have not been studied by dielectric techniques. Since the water potential is an important property of clays for agriculture and civil engineering, dielectric measurements were performed for the sample whose concentration was controlled so that the water potentials of the four samples were kept the same.

## MATERIALS AND METHODS

# Sample preparation

The samples used here were kaolinite from Kagoshima Prefecture (Muraoka, 1951), montmorillonite from Yamagata Prefecture (Sueno and Nakaishi, 1992), allophane (Yoshinaga, 1966), and imogolite (Miyauchi and Aomine, 1966). For the montmorillonite and kaolinite samples, the size fraction of  $<2 \mu m$ was separated by sedimentation. After saturation with

Na by washing five times with a 1 N solution of NaCl, the excess NaCl was removed by centrifugation and the samples were air-dried at room temperature. After oxidation of organic matter in the allophane sample with  $H_2O_2$ , the sample was successively treated with dithionite-citrate (Mehra and Jackson, 1960) and 2% Na<sub>2</sub>CO<sub>2</sub> (Jackson, 1979). The size fraction of  $<2 \mu m$ was obtained from the suspension with a pH of 9. The allophane was Na saturated by following a similar method as used for montmorillonite and kaolinite. The sample was stored under moist conditions. The imogolite sample was prepared in the same way as allophane, except that the value of pH was 4. The samples were mixed with deionized and distilled water obtained from Wittaker Bioproducts, Inc. The water content of each sample was adjusted using a pressureplate apparatus to a water potential of 33 kPa. The resultant water content, on the basis of 110°C oven drying, is: kaolinite, 74.5 wt. %; montmorillonite, 724.3 wt. %; allophane, 175.8 wt. %; imogolite, 2406 wt. %.

# TDR method

Dielectric measurements in the frequency range of 1 kHz to 20 GHz were performed following the TDR method (Cole et al., 1980; Mashimo et al., 1987a). In this method, a step-voltage pulse, with a 30-ps rise time and 200-mV height, generated by a tunnel diode passes through a flexible coaxial cable (Suhner Electrics, Ltd., Sucoform 141PE, 50 Ω, dc: 26.5 GHz) to the sample surface upon which the applied pulse is reflected. The form of the reflected pulse is recorded and digitized by a digitizing oscilloscope (Hewlett Packard, HP54121T, dc: 20 GHz). The wave from was accumulated 128 times for each measurement. As derived by Cole (Cole, 1975a, 1975b; Cole et al., 1980), the complex permittivity of unknown sample  $\epsilon_{x}^{*}(\omega)$ where  $\omega$  is the angular frequency is given by Equation (1) (see Table 1). A similar equation can be obtained for the sample of known permittivity  $\epsilon_s^*(\omega)$  [see Equation (2) in Table 1]. Taking into account the elimination of  $v_0(\omega)$ , combining Equations (1) and (2) gives the estimation of  $\epsilon_s^*(\omega)$  as a function of  $\epsilon_s^*(\omega)$  [see Equation (3) in Table 1].

In this study, a dilute NaCl aqueous solution, which gives the same dc conductivity as the unknown sample, was used as a reference sample. The effects of NaCl concentration on the complex permittivity of water and on the dc conductivity are well known (Winsor and Cole, 1982a, 1982b). If the concentration is <0.1 N NaCl, the complex permittivity is equivalent to that of water. We use  $\epsilon_s^*(\omega) - \sigma/j\omega \epsilon_o$  instead of  $\epsilon_s^*(\omega)$  in Equation (3) where  $\sigma$  is the dc conductivity and  $\epsilon_o$  is the dielectric constant *in vacuo*. The dc conductivity can also be estimated using pure water as the reference from the measurements of the reflected wave over a significantly long period. We employed "time win-

dows" to identify the total dielectric spectrum. Depending on the sample, the longest time window or period was selected so that  $R_s(t) - R_x(t)$  definitely reaches zero. Figure 1a and 1b shows  $R_s(t) - R_x(t)$  of the allophane and kaolinite at the longest time window, respectively. Note that the kaolinite sample has the relaxation process at the lower-frequency region, compared with allophane. If  $t_1$  is defined as the time when  $R_s(t) - R_x(t)$  reaches zero,  $\rho$  in Equation (3) can be described by Equation (4) (Table 1).

Two sample cells with different d and  $\gamma_d$  were employed in this study. For accurate measurements in a frequency range >100 MHz, the shorter cell with d =0.01 mm and  $\gamma_d = 0.13$  mm was used. In the range below 1 GHz, a cell with d = 2.0 mm and  $\gamma_d = 4.54$ mm was used. Time windows employed were 5 and 20 ns for the shorter cell and 50, 100, 200, 500 ns, 1, 2, 5, and 10 µs for the longer cell. By using these cells, even very small relaxation with a relaxation strength of the magnitude of 0.1 may be measured in the frequency region of concern (Umehara et al., 1990). For the overlapping region of frequency between 100 MHz and 1 GHz, data obtained by the two cells were in agreement. Data accumulation was done with five repetitions for the complex permittivity. To obtain a high resolution of frequency, a narrow frequency interval of 0.05 on a logarithmic scale was used.

#### RESULTS

Dielectric-dispersion and absorption curves of moist kaolinite are shown in Figure 2. Two inflections are faintly observed in the dispersion curve near 100 kHz and 100 MHz (Figure 2a), but the corresponding relaxation peak cannot be distinguished from the absorption curve (Figure 2b). The absorption owing to dc conductivity is so large that the small relaxation peaks are not apparent. When the contribution of the dc conductivity is subtracted (Figure 3), the two relaxation peaks appear clearly around those frequency regions, as shown in Figure 3b. Thus, the total dispersion and absorption curves are described well by the sum of three relaxation processes as given by Equation (5) (Table 1). The parameters in Equation (5), determined by least-squares, are listed in Table 2. For montmorillonite, a similar relaxation model explains the total relaxation spectra satisfactorily as shown in Figure 4. The relaxation parameters identified are given in Table 2. The total dispersion and absorption curves for allophane and imogolite were described well by Equations (6) and (7), respectively (Table 1). The determined relaxation parameters are given in Table 2. These parameters based on the best fit explain the total relaxation spectra satisfactorily as shown in Figures 5 and 6 for allophane and imogolite, respectively.

where

Table 1. List of equations.

$$\epsilon_{x}^{*} = \epsilon_{x}'(\omega) - j\epsilon_{x}''(\omega)$$
$$= \frac{c}{j\omega\gamma_{d}} \frac{v_{0}(\omega) - r_{x}(\omega)}{v_{0}(\omega) + r_{x}(\omega)} Z_{x}(\omega) \cot Z_{x}(\omega)$$
(1)

where

$$Z_{x}(\omega) = \left(\frac{\omega d}{c}\right) \epsilon_{x}^{*}(\omega)^{1/2}$$
  

$$\epsilon_{s}^{*}(\omega) = \epsilon_{s}'(\omega) - j\epsilon_{s}''(\omega)$$
  

$$= \frac{c}{j\omega\gamma_{d}} \frac{v_{0}(\omega) - r_{s}(\omega)}{v_{0}(\omega) + r_{s}(\omega)} Z_{s}(\omega) \cot Z_{s}(\omega) \qquad (2)$$

where

$$Z_{s}(\omega) = \left(\frac{\omega d}{c}\right) \epsilon_{s}^{*}(\omega)^{1/2}$$

where the subscripts x and s refer to samples of unknown and known permittivities, respectively;  $\epsilon'(\omega)$  and  $\epsilon''(\omega)$  are functions that produce dispersion and absorption curves of complex permittivity, respectively; *j* represents an imaginary unit; *d* and  $\gamma_d$  are geometrical and effective electrical lengths of the coaxial sample cell, respectively;  $v_0(\omega)$  is the Fourier transform of the incident pulse applied to the sample;  $r(\omega)$  is that of the reflected pulse R(t); and *c* is the speed of propagation *in vacuo*. The term  $Z(\omega) \cot Z(\omega)$  accounts for the multiple reflection in the sample section.

$$\epsilon_{x}^{*}(\omega) = \epsilon_{s}^{*}(\omega) \frac{1 + \{cf_{s}(\omega)/[j\omega\gamma_{d}\epsilon_{s}^{*}(\omega)]\}\rho(\omega)}{1 + \{[j\omega\gamma_{d}\epsilon_{s}^{*}(\omega)]/cf_{s}(\omega)\}\rho(\omega)} \frac{f_{x}(\omega)}{f_{s}(\omega)}$$
(3)

where

$$p(\omega) = \frac{r_{s}(\omega) - r_{x}(\omega)}{r_{s}(\omega) + r_{x}(\omega)} \qquad f_{x}(\omega) = Z_{x}(\omega) \cot Z_{x}(\omega),$$

 $f_{\rm s}(\omega) = Z_{\rm s}(\omega) \cot Z_{\rm s}(\omega)$ 

$$\rho(\omega) = \frac{\int_{0}^{t_{1}} [R_{s}(t) - R_{x}(t)]e^{-j\omega t} dt}{2\int_{0}^{t_{1}} [R_{s}(t)]e^{-j\omega t} dt - \int_{0}^{t_{1}} [R_{s}(t) - R_{x}(t)]e^{-j\omega t} dt}$$
(4)

$$\epsilon^{*}(\omega) = \epsilon_{*} + \frac{\Delta\epsilon_{1}}{(1+j\omega\tau_{1})^{\alpha_{1}}} + \frac{\Delta\epsilon_{m}}{1+(j\omega\tau_{m})^{\beta_{m}}} + \frac{\Delta\epsilon_{h}}{1+(j\omega\tau_{h})^{\beta_{h}}}$$
(5)

$$\epsilon^{*}(\omega) = \epsilon_{\infty} + \frac{\Delta\epsilon_{1}}{(1+j\omega\tau_{1})^{\alpha_{1}}} + \frac{\Delta\epsilon_{m}}{(1+j\omega\tau_{m})^{\alpha_{m}}} + \frac{\Delta\epsilon_{h}}{1+(j\omega\tau_{h})^{\beta_{h}}}$$
(6)

$$\epsilon^{*}(\omega) = \epsilon_{*} + \frac{\Delta\epsilon_{1}}{1 + j\omega\tau_{1}} + \frac{\Delta\epsilon_{h}}{1 + (j\omega\tau_{h})^{\beta_{h}}}$$
(7)

where the subscripts l, m, and h refer to the relaxation process at low, intermediate, and high frequencies, respectively,  $\epsilon_x$  is the dielectric constant extrapolated to  $\omega = \infty$ ,  $\Delta \epsilon$  is the relaxation strength,  $\tau$  is the relaxation time, and  $\alpha$  and  $\beta$  are the Cole-Davidson and Cole-Cole parameters (*e.g.*, Hill *et al.*, 1969) representing the distribution of relaxation times, respectively.

$$\tau_1 = \frac{\epsilon_c'(n-1) + \epsilon_s'}{4\pi\sigma_s}$$
(8)

where  $\epsilon_{c}'$  and  $\epsilon_{s}'$  are the dielectric constant of clay and solution, respectively;  $\sigma_{s}$  is dc conductivity and *n* is a shape factor.

Table 1. Continued.

$$\tau_1 = \frac{\mathbf{r}^2}{2u_1 kT} \tag{9}$$

 $u_1 = u_0 \exp\left(\frac{-E}{kT}\right)$ 

where r is the radius of a spherical particle or the half-length of a rod-shaped particle,  $u_0$  is the sodium volocity per unit force in water, k is the Boltzmann constant, T is the absolute temperature, and E is the potential barrier for the migration.

$$\Delta \epsilon_{i} = \frac{9}{4} \frac{p}{\left(1 + \frac{p}{2}\right)^{2}} \frac{q^{2} r \delta}{\epsilon_{0} k T}$$
(10)

where p is the volume fraction of clay, q is the electronic charge unit,  $\epsilon_0$  is the dielectric constant of the vacuum and  $\delta$  is the charge density.

#### DISCUSSION

#### Non-bound water

The values of the relaxation time  $\tau_h$  for the process at high frequencies at 20 GHz are not dependent on

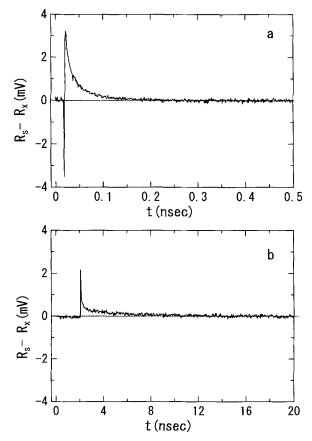


Figure 1. For a long-time range, the time-domain signal  $R_s$  –  $R_x$  reaches zero for (a) allophane and (b) kaolinite.

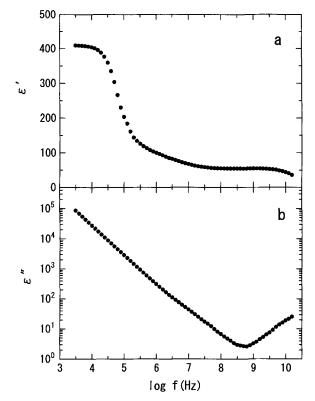


Figure 2. Experimental dielectric-dispersion (a) and absorption curves (b) for moist kaolinite, including the contribution of dc conductivity, f = frequency.

the type of minerals studied here. These values range from 7.1 to 8.9 ps and compare favorably with previously determined values for pure water. For example, comparative values at 20 and 30°C are 9.2 and 7.2 ps, respectively (e.g., Hill et al., 1969). Thus, the process at high frequencies is caused by the reorientation of bulk-H<sub>2</sub>O molecules. Sposito (1981) showed that the dielectric-relaxation time for bulk H<sub>2</sub>O is related to the time constant for the reorientational motion of a single H<sub>2</sub>O molecule, provided H<sub>2</sub>O may be described as a rigid sphere that adheres to the interface. The dielectric-dispersion and absorption curves for all minerals except for montmorillonite are described well by the Cole-Cole representation (Ishida and Makino, 1999a, 1999b). Figure 7 illustrates the relationship between the relaxation strength  $\Delta \epsilon_{\rm h}$  and the water content, showing that the values of  $\Delta \epsilon_{h}$  increase with an increase in water content.

## Bound water

For imogolite, the low-frequency process near 10 MHz is caused by the orientation of bound  $H_2O$  on the imogolite surface, based on relaxation strength and time. The dielectric relaxation is a pure Debye contribution, which indicates that the contribution excludes the distribution of relaxation time, and thus interfacial

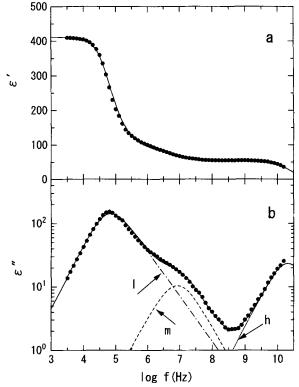


Figure 3. Dielectric-dispersion (a) and absorption (b) curves for moist kaolinite obtained after the contribution of dc conductivity is subtracted.  $\bullet$  reveals the observed data. "h", "m", and "l" refer to the high-, intermediate-, and low-frequency processes, respectively. Solid, dotted, broken, and chain lines show total, "h", "m", and "l" processes, respectively, calculated from Equation (5) by using relaxation parameters listed in Table 2. The mean errors over the frequency (f) of concern are within 3 and 7% for the dispersion and absorption curves, respectively.

polarization is not of interest in this study. If interfacial polarization occurred, the relaxation time is distributed as a result of inhomogeneous interactions of imogolite tubes. The value of  $\tau_1$ , 22 ns, is 1000 times smaller than for pure ice (Hill *et al.*, 1969), whereas it is approximately ten times larger than that of bound H<sub>2</sub>O in biological materials (*e.g.*, Mashimo *et al.*, 1987b).

The values of  $\tau_1$  and  $\alpha_1$  for allophane are similar to those for imogolite. The similarity in  $\alpha_1$  implies that the distribution of relaxation times occurs within a small range. Because the allophane concentration is considerably greater than the concentration of imogolite, the content of bound H<sub>2</sub>O or the relaxation strength for allophane is probably larger than for imogolite. Therefore, the process at low frequencies for allophane is attributed to the orientation of the bound H<sub>2</sub>O. There probably is no other relaxation mechanism at intermediate frequencies for allophane except for the orientation of the bound H<sub>2</sub>O, because only H<sub>2</sub>O is active in dielectric relaxation in this frequency re-

Table 2. Dielectric relaxation parameters in Equations (5)–(7) determined for the four moist samples.

Sample	$\log \tau_i(s)$	Δ ε,	a	$\log \tau_m(s)$	$\Delta \epsilon_{\rm m}$	α <sub>m</sub>	βm
Kaolinite Montmorillonite Allophane Imogolite	$\begin{array}{r} -5.52 \pm 0.38 \\ -6.58 \pm 0.35 \\ -7.51 \pm 0.21 \\ -7.66 \pm 0.24 \end{array}$	$290.6 \pm 22.4 \\ 24.6 \pm 2.8$	**** = ****	$\begin{array}{r} -7.72 \pm 0.21 \\ -8.06 \pm 0.24 \\ -8.69 \pm 0.18 \end{array}$	$\begin{array}{c} 23.6 \pm 1.6 \\ 130.4 \pm 9.3 \\ 5.6 \pm 1.5 \end{array}$	$1.00 \\ 1.00 \\ 0.65 \pm 0.03$	$\begin{array}{c} 0.92\ \pm\ 0.02\\ 0.81\ \pm\ 0.03\\ 1.00\end{array}$

gion. This result implies that two different structures of bound  $H_2O$  are present in allophane. The value of  $\alpha_m$  is significantly smaller than that of  $\alpha_1$ . Henmi (1991) showed that the thermal energy required to remove  $H_2O$  allows a distinction to be made between bound  $H_2O$  inside and outside of allophane spherules. The result of Henmi may support the two different bound-water structures.

For kaolinite and montmorillonite, the intermediatefrequency results are probably caused by bound H<sub>2</sub>O, based on the values of  $\tau_m$ , which are close to those for montmorillonite suspensions (Ishida and Makino, 1999b). However, these values are much smaller than those for Na-rich kaolinite complexes (Hall and Rose, 1978) and much larger than those for Na-rich montmorillonite (Mamy, 1968) at very low-water contents. The relaxation time at intermediate frequencies for kaolinite compares favorably with those for low frequencies for imogolite and allophane, whereas the relaxation time for montmorillonite is approximately twice as long. Based on differential heat measurements of water-vapor adsorption at low relative humidity, Iwata et al. (1989) stated that the affinity of  $H_2O$  for clay-like surfaces increases in the order: montmorillonite, kaolinite, and allophane. Regarding the relaxation time as a rough measure of the interaction of the mineral surface and the bound-H<sub>2</sub>O molecule, the relaxation time obtained in this study is consistent with this order of affinity. The results obtained here also are consistent with Fripiat et al. (1965) relating to the mobility of H<sub>2</sub>O molecules.

The bound H<sub>2</sub>O for kaolinite and montmorillonite has a symmetric distribution of relaxation times, which is reflected by the Cole-Cole representation. The process occurring in the intermediate frequencies for allophane has an asymmetric distribution for the Cole-Davidson representation. The asymmetric distribution is generally observed in the chain motion of coiled polymers. This distribution arises from the correlation between segmental motion (e.g., Harviliak and Negami, 1967). If the bound  $H_2O$  constructs a chain-like structure and the reorienting molecule correlates with neighboring molecules in the chain, the distribution will be asymmetric, similar to that of a chain polymer. If a "card-house" structure with edge-to-face contacts is formed in phyllosilicate minerals such as montmorillonite and kaolinite, then this structure may make the surface of the phyllosilicate energetically heterogeneous to produce a symmetric distribution of relaxation times. The dielectric curves of montmorillonite (Mamy, 1968; Calvet, 1975) and kaolinite (Hall and Rose, 1978) at very low-water contents are also described by the Cole-Cole representation. However, the values of  $\alpha_m$  obtained in the present paper are about twice those obtained at these very low-water contents. The difference in the distribution pattern of relaxation times may indicate that the bound-H<sub>2</sub>O structure on these mineral surfaces is formed in a dissimilar manner between the phyllosilicates and poorly crystalline phases.

Figure 8 shows the relaxation strength owing to bound  $H_2O$  relative to water content. This figure shows that the value of the relaxation strength for montmorillonite is remarkably higher than those for the other three phases. This anomalous property may provide additional understanding for the swelling mechanisms of montmorillonite. The relaxation strength is closely related to the number of bound-H<sub>2</sub>O molecules and the square of the dipole moment. Bound-H<sub>2</sub>O structure is reflected in values of the dipole moment. At present, it is difficult to relate the contributions of each. However, the relaxation strength may relate to a unique aspect about the bound-H<sub>2</sub>O structure on the montmorillonite surface.

### Interfacial polarization

Many workers (e.g., Lockhart, 1980a, 1980b; Sen, 1981) observed large values for dielectric constants in the kHz range. Although these values may be related to polarizations of the double layer surrounding the charged clay particles (Dukhin, 1973), the detailed mechanism responsible for these large values is not understood. The mechanism involves electrochemical effects owing to the electrical properties of clay surfaces, as well as geometrical effects (Sen, 1981) owing to the shape of the particles.

The interfacial polarization may be related to processes occurring in the low-frequency regions for kaolinite and montmorillonite. Raythatha and Sen (1986) showed that the "tail" of the interfacial polarization persists in the MHz frequency range, as was observed here also. However, as discussed above, the relaxation process owing to the rotation of bound H<sub>2</sub>O also appears in this frequency range. Although Raythatha and Sen considered that the contribution of bound H<sub>2</sub>O to the total dielectric relaxation is too small to be important, the contribution is significant (see Figures 3 and 4). This observation results from the high precision of

$\log \tau_h(s)$	$\Delta \epsilon_{\rm h}$	β <sub>h</sub>	€ <sub>∞</sub>
$\begin{array}{r} -11.12 \pm 0.21 \\ -11.15 \pm 0.17 \\ -11.07 \pm 0.23 \\ -11.05 \pm 0.12 \end{array}$	$59.1 \pm 1.4$ $51.8 \pm 2.5$	$\begin{array}{c} 0.98 \pm 0.01 \\ 1.00 \pm 0.00 \\ 0.97 \pm 0.01 \\ 0.98 \pm 0.01 \end{array}$	$5.3 \pm 0.6 \\ 4.2 \pm 0.8 \\ 4.0 \pm 0.7 \\ 5.2 \pm 0.4$

Table 2. Extended.

the dc estimate. Because data are insufficient to determine the interfacial-polarization mechanism quantitatively, we discuss the possible mechanisms in qualitative terms.

The Maxwell-Wagner effect commonly is used to explain the interfacial polarization on clays at lowwater contents, for example, see Calvet (1975) and Helmy *et al.* (1988) for montmorilonite, or Goldsmith and Muir (1960) for kaolinite. We discuss the possibility of using the Maxwell-Wagner model in the form by Sillars (1936) for conducting spheroids in an in-

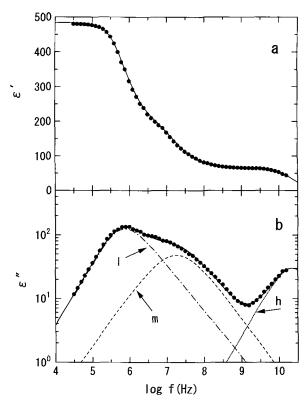


Figure 4. Dielectric-dispersion (a) and absorption (b) curves for moist montmorillonite obtained after the contribution of dc conductivity is subtracted. • reveals the observed data. "h", "m", and "l" refer to the high-, intermediate-, and lowfrequency processes, respectively. Solid, dotted, broken, and chain lines show total, "h", "m", and "l" processes, respectively, calculated from Equation (5) by using relaxation parameters listed in Table 2. The mean errors over the frequency (f) of concern are within 3 and 9% for the dispersion and absorption curves, respectively.

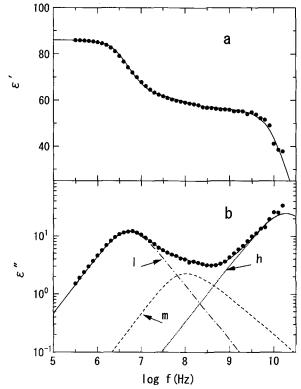


Figure 5. Dielectric-dispersion (a) and absorption (b) curves for moist allophane obtained after the contribution of dc conductivity is subtracted.  $\bullet$  reveals the observed data. "h", "m", and "l" refer to the high-, intermediate-, and low-frequency (f) processes, respectively. Solid, dotted, broken, and chain lines show total, "h", "m", and "l" processes, respectively, calculated from Equation (6) by using relaxation parameters listed in Table 2. The mean errors over the frequency of concern are within 2 and 5% for the dispersion and absorption curves, respectively.

sulating matrix. The relaxation time is given by Equation (8) (Table 1).

If the relaxation time  $\tau_1$  is assumed to be inversely proportional to the dc conductivity, the difference in  $\tau_1$  between kaolinite and montmorillonite can be explained qualitatively by the Maxwell-Wagner effect or by the difference in dc conductivity. The dc conductivity is: kaolinite,  $5.4 \pm 0.5$  mS/m; montmorillonite,  $259.0 \pm 11.3$  mS/m; allophane,  $58.2 \pm 3.9$  mS/m; imogolite,  $11.0 \pm 0.8$  mS/m.

Another possible mechanism is the tangential migration (*i.e.*, surface-polarization effect) of counterions at the clay surface. Recently Ishida and Makino (1999b) performed dielectric measurements on montmorillonite suspensions under various pH conditions. They showed that the surface-polarization mechanism is a more appropriate model for the relaxation process observed at low frequency than the Maxwell-Wagner mechanism, based on the dependence of the relaxation times on dc conductivities. The relaxation time for the

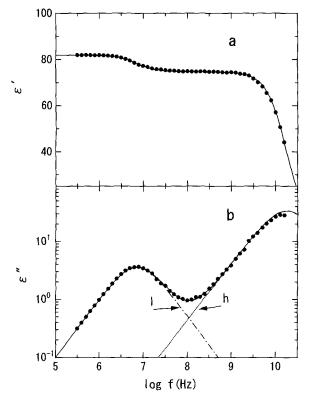


Figure 6. Dielectric-dispersion (a) and absorption (b) curves for moist imogolite obtained after the contribution of dc conductivity is subtracted.  $\bullet$  reveals the observed data. "h" and "l" refer to the high- and low-frequency processes, respectively. Solid, dotted, and chain lines show total, "h", and "l" processes, respectively, calculated from Equation (7) by using relaxation parameters listed in Table 2. The mean errors over the frequency (f) of concern are within 2 and 4% for the dispersion and absorption curves, respectively.

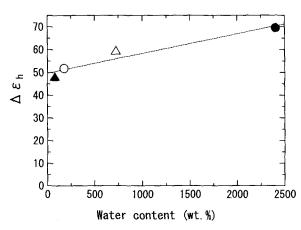


Figure 7. Dependence of  $\Delta \epsilon_h$  on water content.  $\blacktriangle$ , kaolinite;  $\Delta$ , montmorillonite;  $\bigcirc$ , allophane;  $\blacklozenge$ , imogolite.

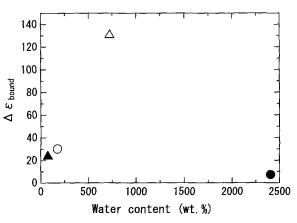


Figure 8. Dependence of relaxation strength owing to bound  $H_2O$  on water content.  $\blacktriangle$ , kaolinite;  $\triangle$ , montmorillonite;  $\bigcirc$ , allophane;  $\bigcirc$ , imogolite.

counter-ion process is described (Schwarz, 1962) by Equation (9) of Table 1. Also, the relaxation strength (Schwarz, 1962) is given by Equation (10) of Table 1. The radius and charge density were estimated based on Ishida and Makino (1999b). The radii obtained are 0.092 and  $0.031 \,\mu$ m for kaolinite and montmorillonite, respectively. The charge densities are 0.00071 and  $0.0025 \,\text{meq/m}^2$ . Those values for montmorillonite are comparable with those in Ishida and Makino (1999b). The comparison in the values between kaolinite and montmorillonite indicates that the surface-polarization mechanism might be qualitatively reasonable (Lockhart, 1980a, 1980b). Therefore, we cannot determine which mechanism is responsible for the interfacial polarization under moist conditions.

However, the Maxwell-Wagner and surface-polarization effects cannot be general mechanisms responsible for interfacial polarization of all the mineral-water systems, because allophane and imogolite do not have a relaxation process despite both having dc conductivity comparable with that for kaolinite. The structure of the diffuse double layer is a key to the question of the general mechanism. A more detailed study of the interfacial polarization would provide useful information on the structure of the diffuse double layer. The information would contribute to the understanding of non-equilibrium electrical phenomena of clays or colloids (Dukhin, 1993).

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