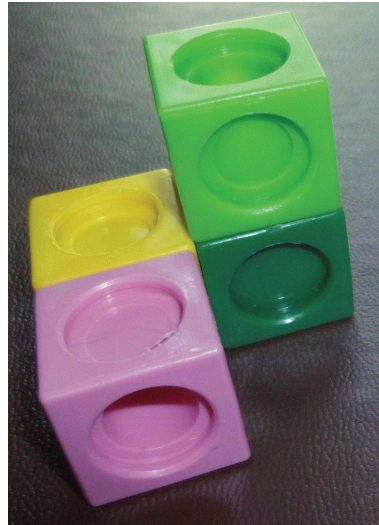




# The Mathematical Gazette



Playing with bricks  
The Presidential Address

Volume 102  
Number 555  
November 2018

MATHEMATICAL ASSOCIATION



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Typeset by Bill Richardson

**CAMBRIDGE**  
**UNIVERSITY PRESS**MIX  
Paper from  
responsible sources  
FSC® C007785

Printed in the UK by Bell &amp; Bain Ltd.

ISSN 0025-5572