

Second-order Total Variation for Compressed Sensing Cryo-ET and Subtomogram Averaging

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Cryo-electron tomography (cryo-ET) is a key tool for imaging macromolecules in cellular environments. Together with subtomogram averaging (STA), cryo-ET can be used for structure determination. Weak visibility of many structures in cryo-ET as well as the volume of data required for STA, however, motivate the exploration of advanced image processing for cryo-ET. Compressed sensing is a mathematically rigorous signal processing approach to sampling with far fewer measurements than traditionally required, with significant applications in limited angle, undersampled electron tomography in the physical sciences [1,2]. Compressed sensing electron tomography (CS-ET) holds that for sample features that can be described as sparse, i.e., those requiring only a few coefficients to represent the object in a particular mathematical transform domain, a set of measurements can be devised to directly identify the tomographic reconstruction that also adheres to that sparsity, in contrast to post-processing approaches. This idea is related to image compression, where an image can be represented by only a small number of coefficients to reduce the storage requirements of the fully sampled image. CS-ET enables reducing data quantities while recovering high-fidelity reconstructions, or provides improved visibility and precision of image features for a given number of samples (measurements) [1–3].

Identifying suitable and general sparse domains for cryo-ET and determining whether these preserve high-resolution structural information is essential. CS-ET has seen several applications in cryo-ET to date [4,5], but high-resolution structures have not been reported. Moreover, advances in CS-ET, including the use of higher order total variation and three-dimensional transforms matched to the three-dimensional object under reconstruction, have not been assessed for cryo-ET. Second-order total variation (CS-TV²) has recently seen wider application in physical sciences CS-ET [6]. Whereas first-order total variation reinforces tomographic reconstructions that are piece-wise constant, structures of interest in cryo-ET exhibit intensity variations with relatively high image density in high-resolution structures, limiting the applicability of sparsity in the image of an object itself. CS-TV² allows for variation in intensity while reinforcing the inherent connectivity of structures in three-dimensions.

To evaluate CS-TV², we first evaluated whether the reconstruction algorithm retains information to the secondary structure level in hepatitis B (HBV) triangulation number (T) = 4 capsid particles [7]. Fig. 1 shows a comparison of WBP and CS-TV² reconstructions, confirming CS-TV² enhances visibility of structures with small fractions of the full dataset and preserves information at the secondary structure level. Application of CS-TV² to *C. crescentus* cells demonstrated that the approach shows wider utility (Fig. 2). In cellular specimens, in particular, the visibility of features is significantly improved in CS-TV² relative to WBP reconstructions. This presentation will discuss important data pre-processing steps, selection of parameters for the evaluated CS-TV² implementation [8], approaches to parallelization, and directions for further development [9].

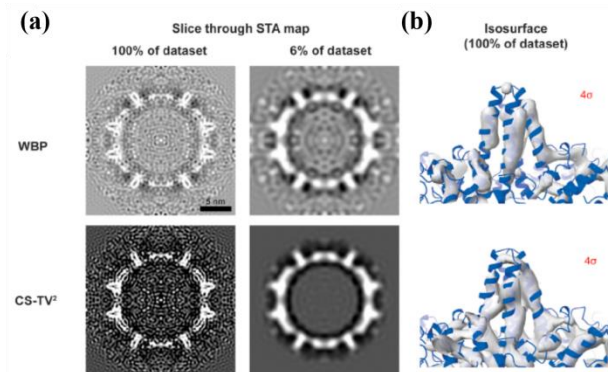


Figure 1. STA results from HBV capsid particles (188 particles at 100%, 12 particles at 6%) shown as (a) orthoslices and (b) isosurface renderings at 4σ isosurface contour level along with an atomic model (PDB: 6HTX) rigid body fitted into the density. Adapted from Ref. [7] (CC-BY).

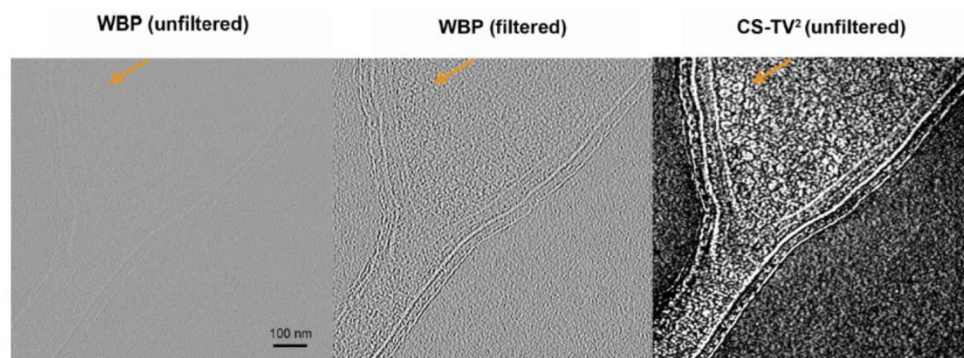


Figure 2. Orthoslices from reconstructions of a *C. crescentus* cell. Adapted from Ref. [7] (CC-BY).

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