

# Recombination lines and maser effects

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**Abstract.** Maser effects occur in recombination lines when the plasma departs from local thermodynamic equilibrium (LTE). Its consequence is not as dramatic as that found in molecular masers, and therefore it is more difficult to recognize. Besides, it occurs in compact high density regions, and its lines fall at millimeter and submillimeter wavelengths, only recently available with good angular resolution. This review will focus on the theoretical aspects of maser recombination lines and on the recent detection of these masers in different astronomical objects.

**Keywords.** masers, radio lines, stars: mass loss, HII regions, jets and outflows

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## 1. Introduction

Radio recombination lines are the result of transitions between atomic energy levels of high quantum number  $n$ . The electrons populate these levels after recombination, and then decay into lower levels, producing the lines.

The first recombination line ( $H90\alpha$ ) towards HII regions was detected at cm wavelengths in 1964 from Pushchino ([Dravskikh & Dravskikh 1964](#)) and in 1965 ( $109\alpha$ ) from NRAO ([Hoglund and Mezger 1965](#)). During the first years, the velocity measured from the radio recombination lines was used to study the spiral structure of our Galaxy.

The intensity of the recombination lines, together with that of the bremsstrahlung continuum radiation was used to determine the physical conditions of the clouds (density and temperature) assuming local thermodynamic equilibrium (LTE) conditions of the gas. It was soon seen that the temperatures obtained from radio recombination lines in large HII regions were smaller than those obtained from optical lines (eg. [Mezger and Hoglund 1967](#)). The reason could be inhomogeneity in the temperature distribution or the assumption of LTE not being valid, implying maser effects ([Goldberg 1966](#)).

The discovery of the first maser in recombination lines occurred in 1989 in the massive star MCW349A ([Martin-Pintado et al. 1989](#)) and later in the massive and evolved star  $\eta$  Carinae ([Cox et al. 1995](#)).

At the time of our last maser meeting in Cagliari, other maser candidates were reported: the source IRS2 in MonR2 ([Jiménez-Serra et al. 2020](#)), and later the Planetary Nebula Mz3, in data obtained with Hershel ([Aleman et al. 2018](#)).

The question is why it took so long for these discoveries, and the answer is that it was necessary to look at the right lines and the right objects.

## 2. Recombination Line Maser Theory

The discovery of masers in recombination lines led to the study of the physical conditions necessary for maser amplification. The first comprehensive study was presented by [Strelitski et al. \(1996\)](#). He considered the radiative transfer across a plane parallel slab of width  $s$ .

The equation of radiative transfer can be written as:

$$\frac{dI_\nu}{d\tau_\nu} = -I_\nu + \frac{j_\nu}{\kappa_\nu}, \tag{2.1}$$

where  $I_\nu$  is the specific intensity at frequency  $\nu$  (energy of the radiation per unit surface, time, frequency and solid angle),  $j_\nu$  is the emission coefficient,  $\kappa_\nu$  the absorption coefficient per unit length, and  $\tau_\nu$  the optical depth, given by:

$$\tau_\nu = \int_0^s \kappa_\nu ds. \tag{2.2}$$

The solution of equation 2.1 is:

$$I_\nu = I_\nu(0)e^{-\tau_\nu} + S_\nu \left[ 1 - e^{-\tau_\nu} \right], \tag{2.3}$$

with:

$$S_\nu = \frac{j_\nu}{\kappa_\nu}. \tag{2.4}$$

$S_\nu$  is called the source function and in thermodynamic equilibrium is equal to the Planck function  $B_\nu(T)$ . In general, the source function contains all the physics: scattering, stimulated emission, non-uniformity, etc.

Let us consider no background radiation, and transition between two levels  $n_1 \rightarrow n_2$  along a slab of depth  $L$ . The source function can be written as:

$$S_\nu = \eta_\nu B_\nu(T), \tag{2.5}$$

with:

$$\eta_\nu = \frac{\kappa_c^* + \kappa_L^* b_2}{\kappa_c^* + \kappa_L^* b_1 \beta_{12}}, \tag{2.6}$$

and

$$\beta_{12} = \frac{1 - \frac{b_2}{b_1} \exp(-h\nu_0/kT_e)}{1 - \exp(-h\nu_0/kT_e)}, \tag{2.7}$$

$b_n$  represents the population of the level of quantum number  $n$  relative to its LTE value,  $\beta_{12}$  is the ratio between the correction factor for stimulated emission and its LTE value and  $\nu_0$  is the rest frequency of the transition.

The level population of the H atoms, relative to their LTE values was calculated with different degrees of accuracy. Initially, only the quantum number  $n$  was considered (Brockelhurs 1970, Walmsley 1990). Storey & Hummer (1995) included later the angular momentum  $l$ , and finally the contribution of the continuum radiation was introduced (Prozesky A. & Smits 2018, Zhu et al. 2019).

Depending on the ratio  $b_2/b_1$ ,  $\beta_{12}$  can be negative. The same is valid for  $\eta_\nu$ , which also depends on value of the absorption coefficients, which can be written as:

$$\kappa_c^* = 6.64 \times 10^{-8} \frac{N_e N_1}{\nu^2} \left( \frac{10^4}{T_e} \right)^{1.5} g_{\text{ff}} \text{ pc}^{-1}, \tag{2.8}$$

$$\kappa_L^* = 1.06 \times 10^{12} \frac{N_e N_i(v)}{\nu} \left( \frac{10^4}{T_e} \right)^{2.5} mK(m) \exp\left( \frac{\xi_n}{kT_e} \right) (\nu\phi_\nu), \tag{2.9}$$

$N_e$  and  $N_i$  are the electron number density of electrons and ions, respectively,  $T_e$  the electron temperature,  $g_{\text{ff}}$  the Gaunt factor for continuum bremsstrahlung,  $mK(m)$  is an approximation to the oscillator strength given by Menzel (1968),  $\xi_n$  the energy of level  $n$

and  $\phi(v)$  the line profile, which takes into account the Doppler, turbulence and pressure broadening.

The total optical depth of the slab to radiation of frequency  $\nu$  is:

$$\tau_{tot} = \tau_c + \tau_L = (\kappa_c^* + \kappa_L^* b_1 \beta_{12}) L \quad (2.10)$$

The intensity at the line center, relative to the continuum is expressed by:

$$r(\nu_0) = \frac{I(\nu_0) - I_c(\nu_0)}{I_c(\nu_0)} = \eta \frac{1 - \exp(-\tau_{tot})}{1 - \exp(-\tau_c)} - 1, \quad (2.11)$$

or

$$r(\nu_0) = \eta \frac{1 - \exp(-\tau_c - \tau_L)}{1 - \exp(-\tau_c)} - 1 \quad (2.12)$$

Depending on the sign of  $\eta$  and the relative values of  $\tau_c$  and  $\tau_L$  we can have different values for  $r(\nu_0)$ . In particular, when  $\eta$  and  $\tau$  are large and negative,

$$r(\nu_0) \approx \frac{|\eta|}{1 - \exp(-\tau_c)} \exp(|\tau_{tot}|). \quad (2.13)$$

Note that  $\eta$  depends only on the physical conditions of the emitting region, while the optical depth depends on the velocity distribution of the material, implying that the length  $L$  can be different for the continuum and for the line, which requires frequency coherence.

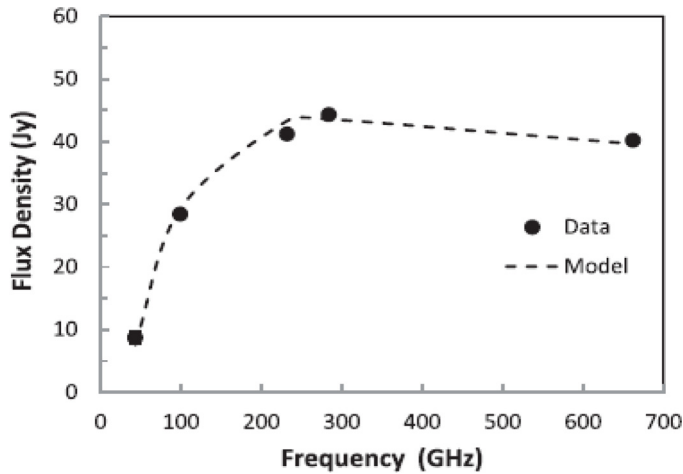
Since  $\tau_{tot}$  is negative, and it is formed by the sum of  $\tau_c$  and  $\tau_L$ , there will be a large difference between the intensity of the recombination lines when the region becomes optically thin, as observed in MCW349A, between the lines H41 $\alpha$  and H30 $\alpha$ .

### 3. Maser Recombination Lines in $\eta$ Carinae

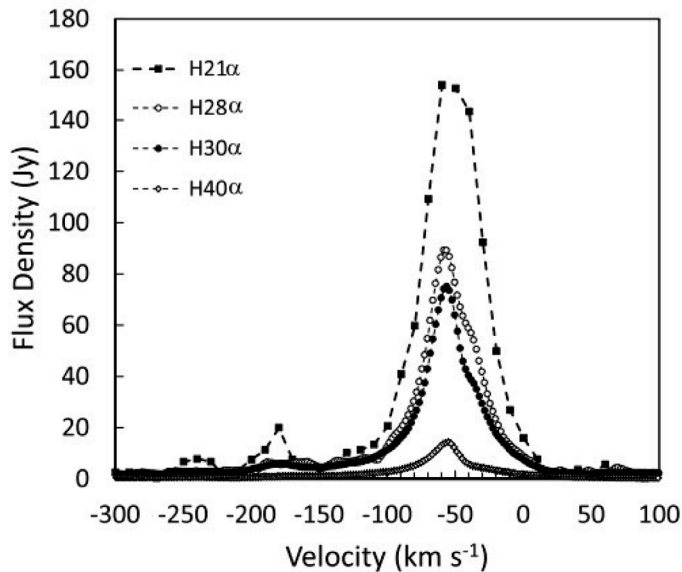
$\eta$  Carinae (hereafter  $\eta$  Car) is the object that presents the strongest recombination line masers detected until now (Cox *et al.* 1995, Abraham *et al.* 2014, 2022). The star, which possibly is in the LBV (Luminous Blue Variable) phase of evolution, underwent a strong episode of mass loss ( $> 30 M_\odot$ ) in 1840; the ejected mass expanded, cooled down and formed the well-known Homunculus Nebula.  $\eta$  Car is part of a binary system in an extremely eccentric orbit, with period of 5.52 years, as revealed by the strictly periodic light curves, observed from radio frequencies to X-ray energies (Damineli 1996, Corcoran *et al.* 2017). The companion star, as well as the photosphere of  $\eta$  Car are not directly visible, because they are embedded in the massive slow wind of  $\eta$  Car, but the companion (probably a Wolf-Rayet star) is believed to have a fast wind of its own; the wind-wind collisions produce shocks that are the origin of the X-ray emission.

Interferometric observations of the binary system at cm wavelengths obtained with the Australian Compact Array (ATCA) revealed extended continuum emission from the surroundings of the binary system, coincident with the Homunculus Nebula, and a disk like structure at the core, with an extension and intensity that varied with the phase of the binary orbit (Duncan & White 2003). This structure was interpreted as gas ionized by the hot companion star, which provided a number of ionizing photons that varied with the orbital phase.

Although cm wave recombination lines were also observed together with the continuum emission, only mm wave lines, observed with the SEST radiotelescope with arcsec resolution, presented strong maser effects, first attributed to the dense wind of  $\eta$  Car (Cox *et al.* 1995). These maser sources presented a single line, contrary to what is observed in the other maser sources, which were modeled as a combination of a Keplerian disk and wind ejected from the disk (Báez-Rubio *et al.* 2013, Jiménez-Serra *et al.* 2020).



**Figure 1.** Continuum spectrum of  $\eta$  Car obtained with ALMA on 2014 (Abraham *et al.* 2014).



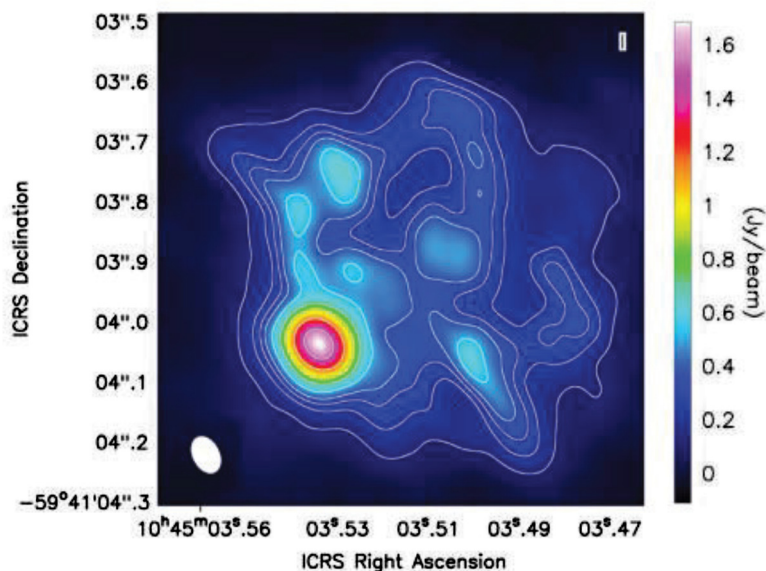
**Figure 2.** Recombination line spectra of  $\eta$  Car obtained with ALMA on 2014 (Abraham *et al.* 2014).

$\eta$  Car was observed with ALMA on 2012 (cycle 0) in the recombination lines H42 $\alpha$ , H40 $\alpha$ , H30 $\alpha$ , H28 $\alpha$ , and H21 $\alpha$  (Abraham *et al.* 2014), but it was not resolved, even at the higher frequencies, where the beam size was  $0.35 \times 0.42$  arcs (at the distance of  $\eta$  Car 50 mas correspond to 110 au).

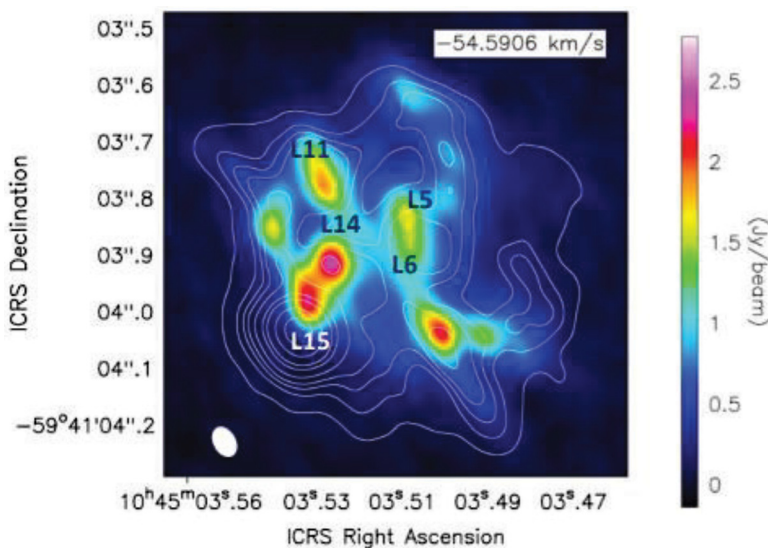
The continuum spectrum is compatible with that of an HII region, with a turnover frequency close to 300 GHz, as can be seen in Figure 1.

In Figure 2 we show the superimposed spectra of the H40 $\alpha$ , H30 $\alpha$ , H28 $\alpha$ , and H21 $\alpha$  lines.

Based on the cm wave observations, which were modeled as originated in an expanding source, the mm wave continuum and lines were modeled as arising from an expanding shell of radius  $R = 6.6 \times 10^{15}$  cm, width  $\Delta R = 0.1R$ , electron density  $N_e = 1.3 \text{ km s}^{-1}$  and temperature  $T_e = 1.7 \times 10^4$  K, expanding with a bulk velocity of  $53 \text{ km s}^{-1}$ , with



**Figure 3.** 230 GHz continuum image of  $\eta$  Car obtained with ALMA on 2017 (Abraham *et al.* 2020).

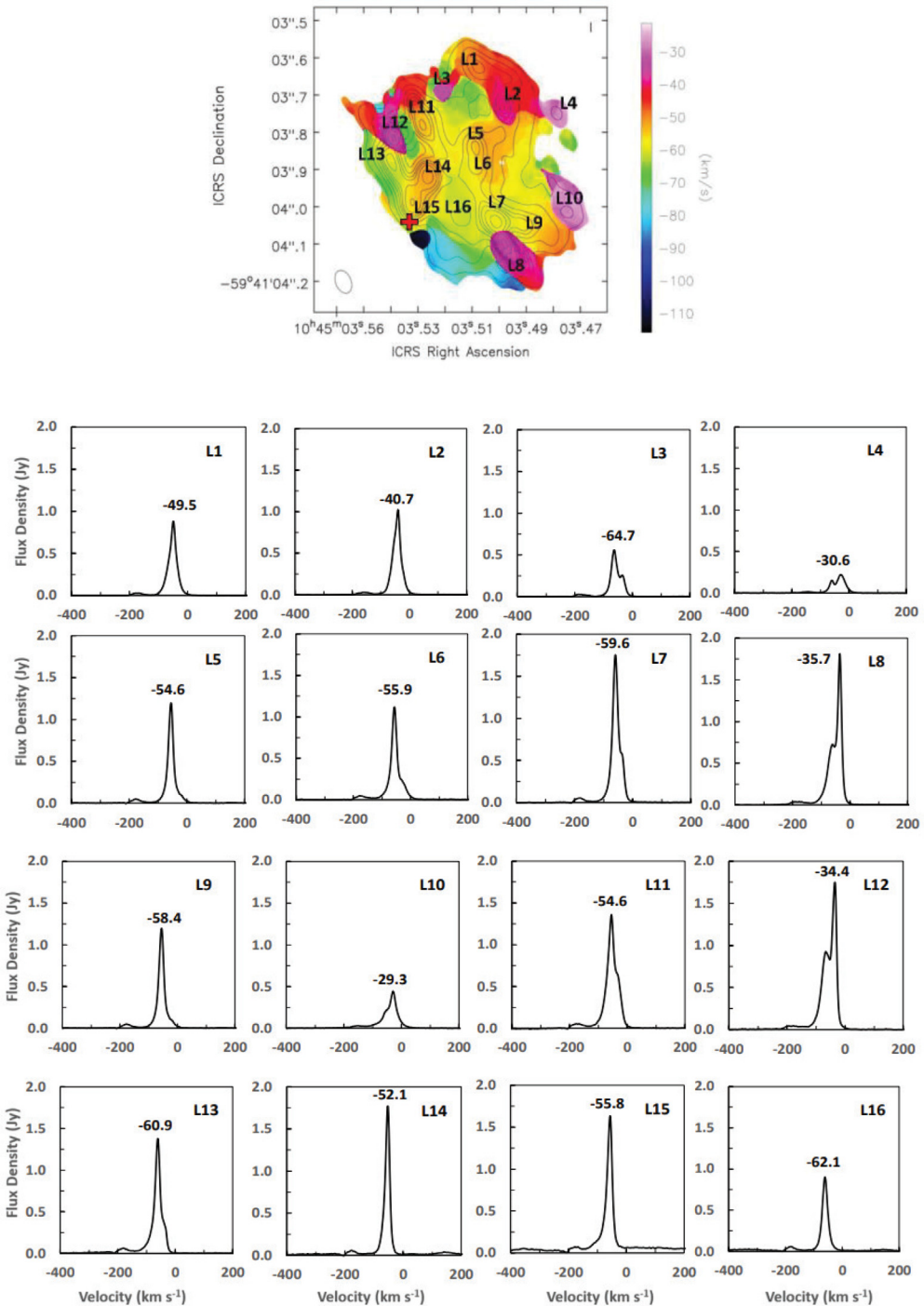


**Figure 4.** Iso-velocity image of the recombination line  $H30\alpha$ , centered at the velocity of  $-54.6 \text{ km s}^{-1}$  and resolution of  $1.3 \text{ km s}^{-1}$ , of  $\eta$  Car obtained with ALMA on 2017 (Abraham *et al.* 2020).

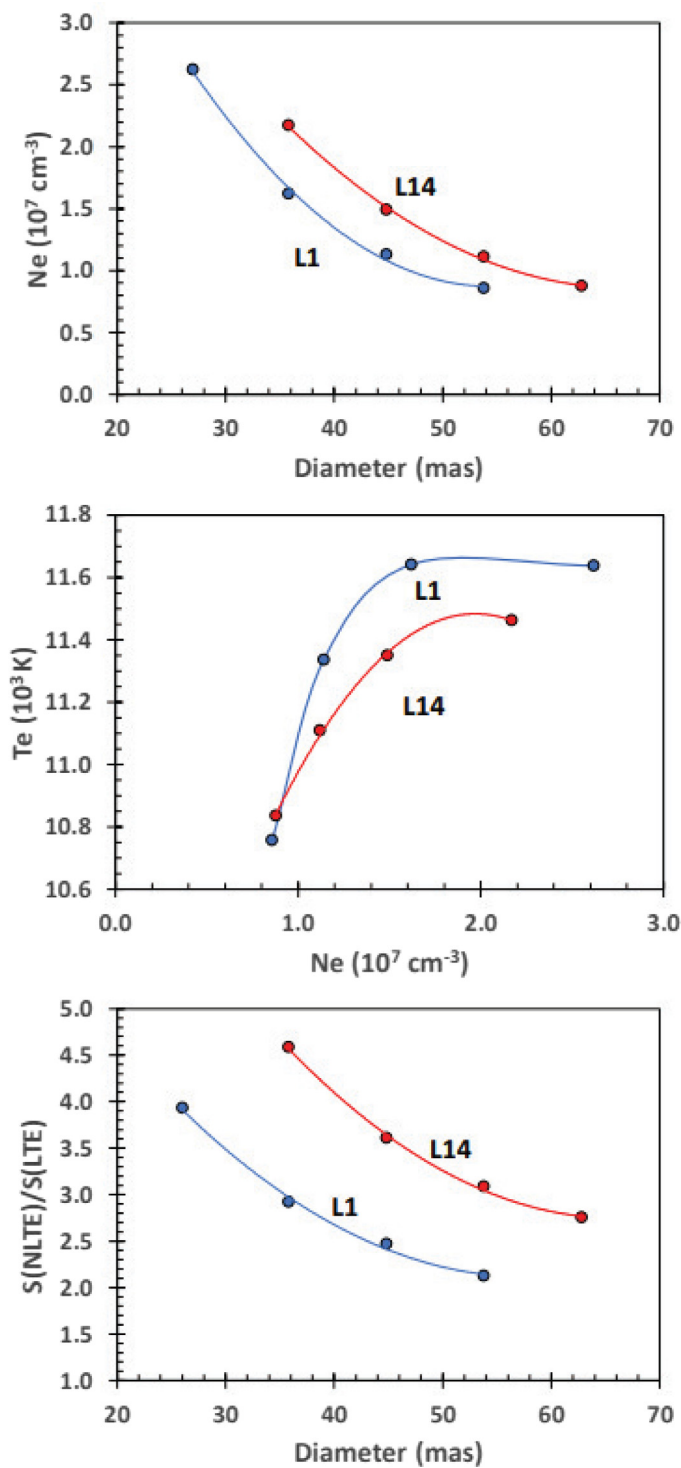
the velocity ranging from  $60 \text{ km s}^{-1}$  to  $20 \text{ km s}^{-1}$  in the inner and outer borders of the shell, respectively.

However,  $\eta$  Car was observed again with ALMA in the 230 GHz continuum and in the  $H30\alpha$  recombination line on 2017, with resolution  $65 \times 43 \text{ mas}$ , and the expanding shell model was not confirmed.

In fact, the continuum emission showed a compact source, centered on  $\eta$  Car and extended emission in the NW direction, as can be seen in Figure 3.



**Figure 5.** Spectra of the 16 compact component identified in the H3 $\alpha$  images of  $\eta$  Car detected with ALMA in 2017. (Abraham *et al.* 2020).



**Figure 6.** Physical conditions of the clumps that fit the spectra of the  $\text{H}30\alpha$  recombination line of clumps 1 and 14, as identified in Figure 5.



The iso-velocity intensity maps of the different velocity channels, with width of  $1.3 \text{ km s}^{-1}$ , revealed several compact (not resolved) components with different velocities on top of the 230 GHz continuum emission. One of these maps, centered at the velocity of maximum emission is shown in Figure 4.

In Figure 5 we show the profiles of the different clumps, identified in the image of the first intensity momentum superimposed on the raster image of the line velocity. We can see that the positions and velocities of the clumps are not compatible with the model of an expansion shell.

Since the maser sources are not resolved, the physical conditions of two of them, labeled as 1 and 14, were investigated for different values of the radius (smaller than 50 mas or 110 ua), assumed to be spherical and homogeneous clumps. The results are shown in Figure 6.

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