

**INSTABILITY, CHAOS
AND PREDICTABILITY IN
CELESTIAL MECHANICS
AND STELLAR
DYNAMICS**

Edited by K.B. Bhatnagar

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DEDICATIONS

It is with great reverence that we dedicate this volume to Lord Shiva—
The Hindu God.

"In classical Hindu Mythology the Cosmos passes through three major phases—creation, maintenance, destruction—mirroring birth-life-death. Brahma is the god of creation, Vishnu the god of maintenance (order), and Shiva the god of destruction (disorder). But Shiva's personality is multifaceted. Shiva is who walks on the wild side, the lone hunter, the dancer, the Yogin who withdraws from human society, the ascetic covered in ash. The untamed. The distinction between the order of Vishnu and the disorder of Shiva is not that of good or evil. It represents instead two different ways in which divinity makes itself manifest; benevolence and wrath, harmony and discord.

Similarly order and chaos in Mathematics are two distinct manifestation of an underlying determinism. And neither exists in isolation".

(Does God play dice?—Stewart, I.)

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