

**TRANSACTIONS**

**OF THE**

**ROYAL SOCIETY OF EDINBURGH.**

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## CONDITIONS OF THE KEITH PRIZE.

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This Prize, the interest of a sum which now amounts to about £800, left by the late ALEXANDER KEITH, Esq. of Ravelston and Dunnottar, will be awarded by the President and Council of the Royal Society of Edinburgh, on the following conditions :—

I. The author of the best paper on a scientific subject (preference being, in all cases given to a paper containing an important discovery in science made in any part of the world), communicated in the first instance to the Royal Society during the sessions 1851–2, 1852–3, or any two succeeding sessions, shall be entitled to the biennial interest of the KEITH FUND, accruing in the respective periods.\*

II. The form of the Prize shall be a Gold Medal, of not more than Fifteen Guineas value. The remainder of the sum shall be given in money, to be spent in Plate or otherwise, at the discretion of the receiver.

III. The award being duly intimated to the receiver of the Prize, he is to apply forthwith to the Treasurer of the Society for payment of it; and, failing to do so within six months of the date of the intimation, he shall forfeit the money, but shall be entitled to receive the Medal.

\* The proceeds of all preceding biennial periods have, in accordance with the decision of the President and Council, been either awarded to scientific individuals, or added to the capital sum.