

THE EMPIRICAL PERIOD-RADIUS RELATION FOR PULSATING STARS : A SYNTHESIS  
 BASED ON PHOTOMETRIC AND RADIAL VELOCITY MEASUREMENTS

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The relation existing between the radius and the period for the pulsating stars of a given class constitutes a powerful test for the theory of stellar evolution and for the identification of the pulsation modes. In recent years, several authors have determined the mean radius of a lot of pulsating stars of various classes by applying the Baade-Wesselink method. Fig. 1 presents the resulting general  $\log P - \log R$  diagram grouping these determinations. The sources for the radii are given by Burki and Meylan (1986). The variable stars in known binaries have been excluded since the presence of a companion biases the radius calculation (Burki, 1984). The determinations marked by arrows are based on the radial velocities by CORAVEL (1m telescope at the Haute-Provence Observatory, France) or/and on the photometry in the Geneva system (40cm and 70cm telescopes at La Silla Observatory, Chile).

For the classical cepheids, two linear regressions have been calculated:

$$\begin{aligned} \log R &= 1.16 + 0.72 \log P & P < 10d & (1) \\ \log R &= 1.03 + 0.77 \log P & P > 10d & (2) \end{aligned}$$

The difference between these two relations, if really significant, could be due to the mass loss process affecting the evolution of massive stars (Burki, 1985). For the cepheids with  $P < 10d$ , the various theoretical models yield a mean relation  $\log R = 1.18 + 0.69 \log P$  (Ferne, 1984), which is quasi-identical with (1). This allows one to derive, from the definition  $Q = P(\bar{\rho}/\rho_{\odot})^{1/2}$ , an equation relating  $Q$ ,  $R$  and  $M$  (mass) :

$$Q = 0.0238 M^{0.5} R^{-0.1} \quad P < 10d \quad (3)$$

For the population II cepheids (BL Herculis and W Virginis stars), the relation is:

$$\log R = 0.87 + 0.54 \log P \quad (4)$$

and it is remarkable to see that this relation satisfies globally well the RR Lyrae,  $\delta$  Scuti and SX Phoenicis stars. By adopting  $0.6 M_{\odot}$  for the typical mass of the population II cepheids and RR Lyrae stars (Harris, 1985), the following relation can be deduced :

$$\log Q = -1.4 + 0.2 \log P \quad (5)$$

In Fig. 1 is also shown the location of FG Sge, the nucleus of a planetary nebula for which Mayor and Acker (1980) derived a value of the mean radius for the years 1978-1979.

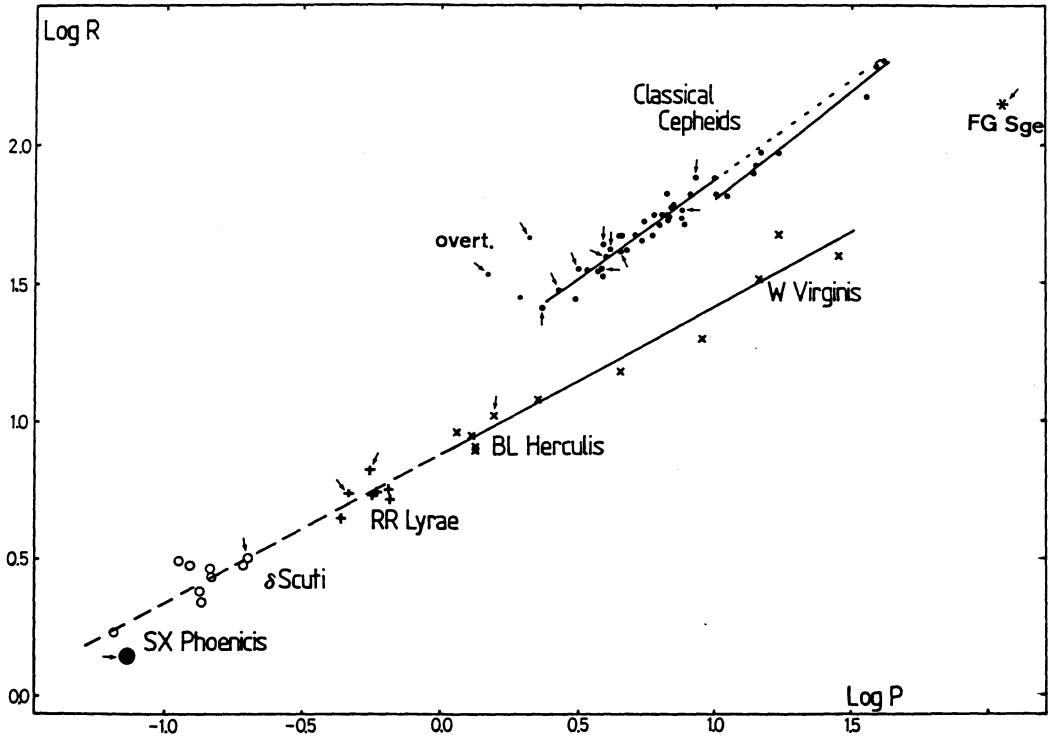


Figure 1. The  $\log R - \log P$  relations for pulsating stars.

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