

PROCEEDINGS
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CAMBRIDGE PHILOSOPHICAL
SOCIETY

VOL. XXIII

PART VIII

(WITH TITLE-PAGE, TABLE OF CONTENTS,
AND INDEX TO VOL. XXIII)

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CAMBRIDGE PHILOSOPHICAL SOCIETY
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