

## A Novel Method for Suppression of Aliasing Ghosts

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**ABSTRACT.** This paper proposes a "half-sample delay switching" to suppress aliasing ghosts caused by finite frequency sampling without the clumsiness of a sharp anti-aliasing filter.

Nyquist theorem says that signals beyond  $R_s/2$  will be overlaid over in-band signals, where  $R_s$  is the sampling rate. Any anti-aliasing filter leaks undesired out-band spurious signals. And "good" sharp-cut filters are usually big and not simple. Are there no ways to suppress aliasing-ghosts without the clumsiness of big anti-aliasing filters? Yes. It is "delay switching".

Consider a cross-power spectrum analyzer for a two-element interferometer, and assume stationary signals and complex-samplers (Figure). When we put a delay  $\delta$  before one of the samplers, there is phase shift  $\Delta\phi$  in the output phase spectrum which is proportional to the input frequency. When the delay  $\delta$  is a half of the sampling period  $1/f_s$ , the phase shifts have a difference of  $180^\circ$  between two signals which are:

- (1). In-band signal of frequency  $f$ .
- (2). Aliasing signal of frequency  $f_a$ , where  $f_a = f + f_s$ .

$$\begin{aligned}\Delta\phi(f) &= 2\pi f\delta \\ &= \pi f/f_s.\end{aligned}$$

$$\begin{aligned}\Delta\phi(f_a) &= 2\pi f_a\delta \\ &= \pi(f+f_s)/f_s \\ &= \Delta\phi(f) + \pi.\end{aligned}$$

The  $180^\circ$  phase shift difference  $\Delta\phi(f_a) - \Delta\phi(f)$  is not affected by delay compensation of phase slope  $\exp(-\pi i f/f_s)$  at the output of the analyzer, because both in- and out-band signals appear in the same frequency channel. Therefore, by adding the compensated output of the delay-on state to the output of delay-off state, we get aliasing-free spectrum. To get precise suppression, put half-sample clock skew circuit ( $0^\circ/180^\circ$  switching of sampling clock, Figure) instead of analog half-sample delay in the signal path. Then we have:

- (1). Precise half-sample delay by simple circuit in any sampling frequency.

(2). No gain/phase change between on- and off-state of the delay switch.

Half-sample delay switching does not discriminate the aliasing ghost whose frequency is separated from the in-band signal by  $k \times f_s$  where  $k$  is an even number. These ghosts can be discriminated by  $m/n$  sample delay switching, for an example,  $0/3-1/3-2/3$  sample delay switching.

Ghost caused by unbalance in a pair of real- and imaginary-part ADC is an aliasing ghost from the negative frequency band. Therefore it can also be suppressed by the delay switching. In the extreme case of the unbalance, aliasing in a case of real-sampling can also be suppressed by the delay switching.

New ADC system of the Nobeyama FX will have this half-sample clock skew switching facilities in 1987.

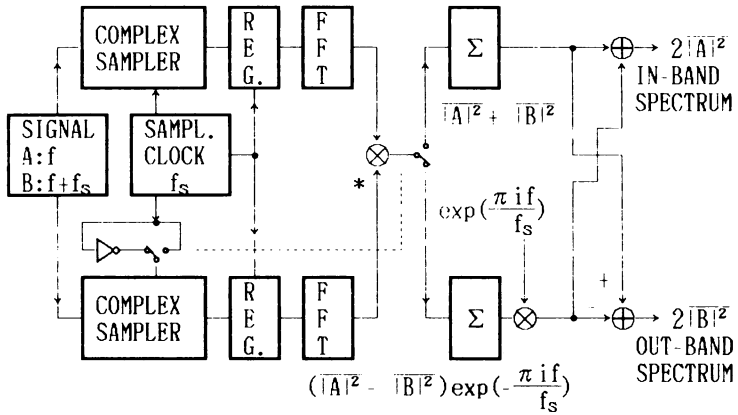


Figure. Block diagram of the half-sample delay ( $1/2 f_s$ ) switching to eliminate aliased out-band spectrum.