

Session 3: Diagnostics of High Gravity Objects with X- and Gamma Rays

3-2. Black Hole Binaries

A MODEL FOR A THIN MAGNETISED DISC IN LMC X-3

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1. Introduction and summary

A model for the stationary radial distribution of the magnetic energy-stress tensor $\langle \mathbf{B}\mathbf{B} \rangle$ in a standard thin disc is presented, with allowance for magnetic torques and dissipation, see Fig. 1. The model is an extension of earlier work by Schramkowski et al. (1996). For LMC X-3, $\langle B^2 \rangle^{1/2}$ reaches $\sim 4 \times 10^5$ G near the inner edge of the disc, and the magnetic pressure is much smaller than the sum of gas and radiation pressure.

2. Equations for a magnetised thin disc

A description of \mathbf{B} in terms of $\langle \mathbf{B}\mathbf{B} \rangle$ permits to allow for: (1) small-scale fields, (2) the influence of magnetic stresses on accretion, and (3) magnetic heating of a disc corona. The relevant equations are (Hoyng 1998):

$$(\partial_t - \beta \nabla^2) \varepsilon = (2\gamma - \zeta \Omega) \varepsilon - 3\Omega m \quad (1)$$

$$(\partial_t - \beta \nabla^2) m = (-\frac{2}{5}\gamma - \zeta \Omega) m - \frac{1}{2}\Omega \varepsilon, \quad (2)$$

where

$$\varepsilon \equiv \langle B^2 \rangle / 8\pi; \quad m \equiv \langle B_r B_\theta \rangle / 8\pi, \quad (3)$$

with $\beta = \frac{1}{3} \langle v^2 \rangle \tau_c$ and $\gamma = \frac{1}{3} \langle |\nabla \times \mathbf{v}|^2 \rangle \tau_c$ (\mathbf{v} is the turbulent flow); $\zeta = \nu/\beta$ is the turbulent Prandtl number and ν is the kinematic viscosity. The terms in (1) and (2) describe turbulent transport (β), amplification due to random field line stretching (γ), resistive dissipation ($\zeta\Omega$), and amplification by the keplerian shear flow Ω . No α -effect has been included.

The disc is modelled with the usual thin disc equations; those for energy and angular momentum have extra terms accounting for heating due to resistive dissipation and for magnetic stresses ($f = 1 - (r_0/r)^{1/2}$):

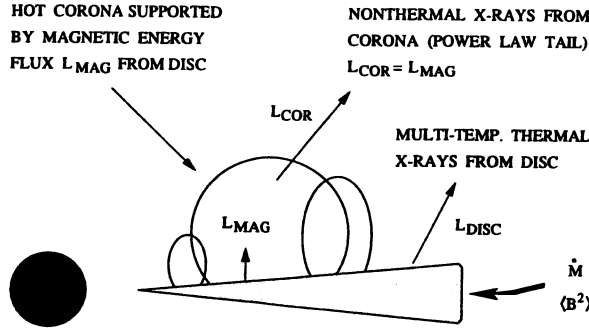


Figure 1. An optically thick magnetised disc in LMC X-3 radiates a multi-temperature blackbody X-ray spectrum. Like in the case of the solar corona, a magnetic flux density $-\beta\partial\epsilon/\partial z$ supports a hot, optically thin corona emitting non-thermal Bremsstrahlung (the hard component of the X-ray spectrum).

$$\frac{4\sigma T^4}{3\tau} = \frac{1}{2}\nu\Sigma \left(r \frac{\partial\Omega}{\partial r} \right)^2 + \frac{1}{2}\zeta\Omega \int_{-H}^H \epsilon dz \tag{4}$$

$$\frac{\dot{M}\Omega f}{2\pi} = -\nu\Sigma r \frac{\partial\Omega}{\partial r} - 2 \int_{-H}^H m dz \tag{5}$$

By separating the vertical co-ordinate z in (1) and (2), two PDE's for ϵ and m in the central plane $z = 0$ are obtained, which are coupled to the algebraic thin disc equations that also refer to $z = 0$. Nonlinear effects are accounted for indirectly, by tuning (1) β so that the growth rate of the fundamental mode is zero, and (2) the constant determining the magnitude of $\epsilon(r)$ so that the sum of the disc luminosity L_{disc} and magnetic luminosity L_{mag} equals the gravitational energy liberated during accretion.

3. Application to LMC X-3

The stationary solution applicable to LMC X-3 features: (1) a maximum r.m.s. field strength $\langle B^2 \rangle^{1/2}$ of 4×10^5 G at $r = 2r_0 = 6r_s$; (2) a $\langle B_r B_\theta \rangle$ that is always negative, while $\epsilon/\rho c_s^2 \lesssim 0.09$; (3) $L_{mag}/L_{disc} \simeq 0.02$, implying that the nonthermal X-ray flux should also be about 0.02 of the thermal X-ray flux, as is observed (Treves et al. 1990; Ebisawa et al. 1993).

References

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