

Incorporating Inelastic Scattering into Multislice Simulation

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Existing Scanning/Transmission Electron Microscopy (S/TEM) image simulation algorithms such as *Multislice* and *Bloch Wave* are based exclusively on elastic scattering. At thicker specimens inelastic scattering may affect image intensity and contrasts. Previous semi-quantitative incorporation of inelastic plasmon scattering into the output of *Multislice* simulated diffraction patterns has improved the agreement between experimental and simulation results from $\sim 30\%$ to less than 10% [1]. In this study, a full quantitative plasmon scattering algorithm was incorporated into *multislice* method [2] by allowing the wavefunction of the propagating beam to interact inelastically within each slice [3].

Crystalline Si samples with 4×4 nm supercells oriented along $\langle 100 \rangle$ crystallographic direction with various thicknesses were used in this simulation. STEM operated at 100 kV accelerating voltage and 11.4 mrad convergence angle giving about 2 Å diameter probe was used here. High-angle annular dark-field (HAADF) STEM images and Electron Energy Loss Spectroscopy (EELS) signals were calculated. For HAADF-STEM images 54 - 150 mrad detector was used and 20 mrad collection angles was used for EELS.

The modified “inelastic-elastic” multislice method first takes into account the plasmon scattering by calculating the energy loss for each scattering angles before undergoing the elastic scattering through transmission operation. Then beam propagates to the next slice using propagation operator. Simulated EELS spectra in Si using new “inelastic-elastic” multislice method for thicknesses of 42, 74, 83, and 130 nm are shown in Figure 1 comparable with early experiments performed under similar conditions [4]. An energy dispersion of 1 eV (for energy loss up to 60 eV) was used in the simulation to monitor single, double, and triple plasmon scattering in these Si samples. A good agreement was achieved for the range of specimen thicknesses.

Figure 2 shows simulated HAADF-STEM images under different *multislice* modes. The simulated image of the Si(100) unit cell for 42 nm thick sample without inelastic scattering is shown in Figure 2(a). For efficient computational time, only a quarter of the unit cell was studied (Figure 2(b)). The “inelastic-elastic” simulated image of the same area is shown in Figure 2(c). The contribution from inelastic scattering is still small at this thickness resulting in only small changes in the image intensity. Hence, Figure 2(b) and (c) look somewhat similar. Additionally, the inelastic scattering intensity collected by the HAADF detector can be analyzed separately using this “inelastic-elastic” multislice algorithm (Figure 2(d)). Thicker specimens are expected to display more significant contributions to the HAADF-STEM signals. The calculated image intensity and contrast could be improved considerably by incorporating these inelastic scatterings into multislice algorithm [5].

References:

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- [4] K.A. Mkhoyan et al., *Ultramicroscopy*, **107** (2006) 345.

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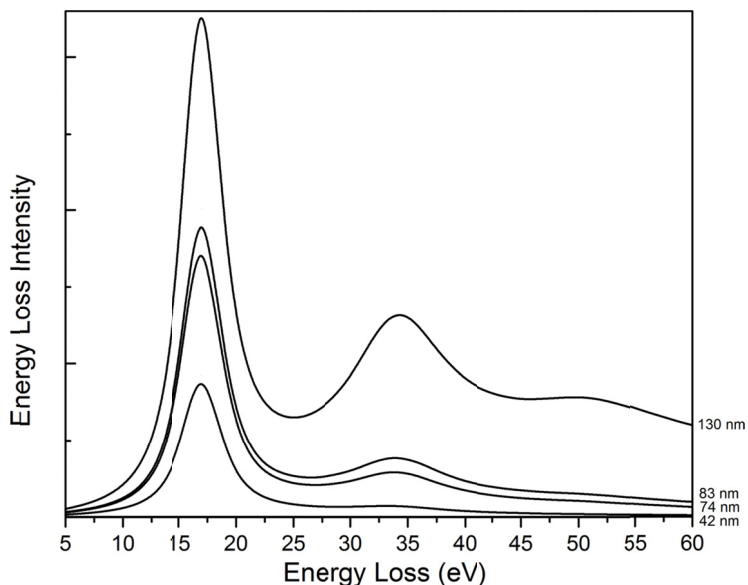


Figure 1. Simulated EELS spectra of Si(100) using the modified “inelastic-elastic” *multislice* method. The collection angle is 20 mrad with samples thicknesses of 42, 74, 83, and 130 nm.

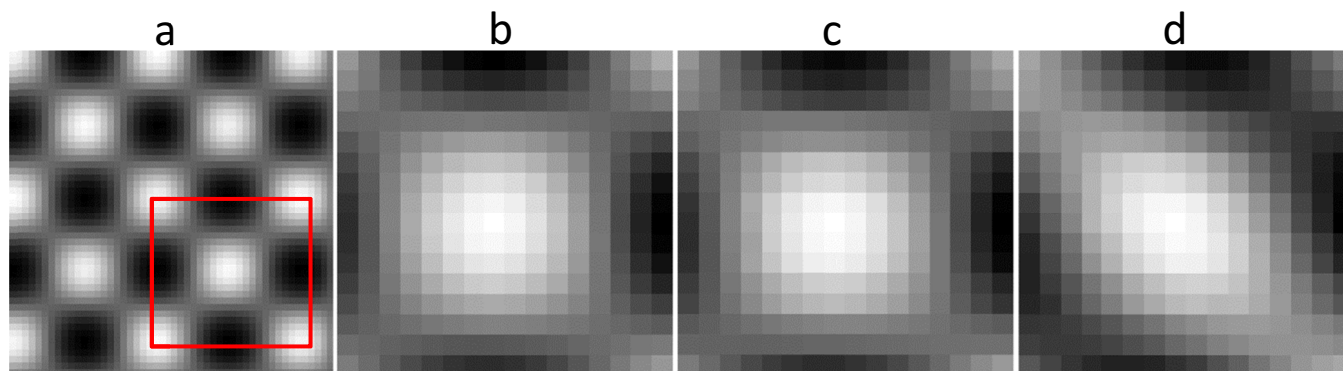


Figure 2. Simulated HAADF-STEM images of 42 nm thick Si(100) crystal. (a) HAADF-STEM image of a unit cell calculated using only elastic scatterings, (b) close-up of the image in (a) (red-boxed region), (c) HAADF-STEM image of the same region as in (b) calculated using “inelastic-elastic” method, and (d) HAADF-STEM image of the same region as in (b) calculated using only inelastic scattered electrons. The images are individually normalized to gray-scale.