

Thermal boundary layer dynamics in low-Prandtl-number Rayleigh–Bénard convection

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In this experimental study, we explore the dynamics of the thermal boundary layer in liquid metal Rayleigh–Bénard convection, covering the parameter ranges of $0.026 \le$ Prandtl numbers (*Pr*) \leq 0.033 and Rayleigh numbers (*Ra*) up to 2.9 \times 10⁹. Our research focuses on characterising the thermal boundary layer near the top plate of a cylindrical convection cell with an aspect ratio of 0.5, distinguishing between two distinct regions: the shear-dominated region around the centre of the top plate and a location near the side wall where the boundary layer is expected to be affected by the impact or ejection of thermal plumes. The dependencies of the boundary layer thickness on *Ra* at these positions reveal deviating scaling exponents with the difference diminishing as *Ra* increases. We find stronger fluctuations in the boundary layer and increasing deviation from the Prandtl–Blasius–Pohlhausen profile with increasing *Ra*, as well as in the measurements outside the centre region. Our data illustrate the complex interplay between flow dynamics and thermal transport in low-*Pr* convection.

Key words: Bénard convection, plumes/thermals, boundary layer structure

1. Introduction

Rayleigh–Bénard (RB) convection, characterised by the natural circulation of a fluid between two horizontal plates subjected to a temperature difference, is a fundamental phenomenon in fluid dynamics with significant implications for various industrial and geophysical processes (Rayleigh [1916;](#page-10-0) Siggia [1994;](#page-10-1) Bodenschatz, Pesch & Ahlers [2000;](#page-9-0) Ahlers, Grossmann & Lohse [2009;](#page-9-1) Chillà & Schumacher [2012\)](#page-9-2). A fundamental parameter in characterising RB convection (RBC) is the Rayleigh number $(Ra = g\beta \Delta T H^3/(\nu \kappa))$, representing the ratio of the buoyancy and viscous forces in the fluid. Here, *g* is the acceleration due to gravity, β is the coefficient of thermal expansion, ΔT is the temperature

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© The Author(s), 2024. Published by Cambridge University Press. This is an Open Access article, distributed under the terms of the Creative Commons Attribution licence [\(http://creativecommons.org/](http://creativecommons.org/licenses/by/4.0) [licenses/by/4.0\)](http://creativecommons.org/licenses/by/4.0), which permits unrestricted re-use, distribution and reproduction, provided the original article is properly cited. 994 A4-1 difference between the plates, *H* is the distance between the plates, ν is the kinematic viscosity and κ is the thermal diffusivity.

The dynamics of the thermal boundary layer (BL) in RBC plays a crucial role in understanding heat transfer mechanisms because the main temperature drop occurs across the BLs which therefore constitute the main resistance for global heat transport (Shraiman & Siggia [1990;](#page-10-2) Grossmann & Lohse [2000;](#page-9-3) Sun, Cheung & Xia [2008\)](#page-10-3). In recent years, significant attention has been paid to investigations of the BL dynamics (Wagner, Shishkina & Wagner [2012;](#page-10-4) Zhou & Xia [2013;](#page-11-0) Scheel & Schumacher [2014\)](#page-10-5). A special feature of the RBC is that, unlike channel flow, the fluid does not flow continuously along the wall. Three different regions result from the fact that thermal plumes coming from the bulk impinge at the plate (plume impact), and detach at a certain distance from the impact zone (plume ejection), whereas in geometries of laterally confined RBC, the detachment area usually occurs at the opposite end of the plate. Impact and ejection zones are connected by a shear flow across the central area (shear-dominated) (van der Poel *et al.* [2015;](#page-10-6) Schumacher *et al.* [2016;](#page-10-7) Scheel & Schumacher [2017;](#page-10-8) Pandey [2021\)](#page-10-9). The local thickness of the thermal BL is the smallest just after the impact zone and grows in the large-scale circulation (LSC) plane towards the opposite sidewall (Wagner *et al.* [2012;](#page-10-4) Pandey [2021\)](#page-10-9). Furthermore, the mean temperature profile near the wall displays deviations from the Prandtl–Blasius–Pohlhausen (PBP) profile, a phenomenon particularly pronounced with smaller Prandtl numbers $(Pr = v/k)$ and larger Ra (van Reeuwijk, Jonker & Hanjalic´ [2008;](#page-10-10) Shishkina *et al.* [2015;](#page-10-11) Ching *et al.* [2019;](#page-9-4) Tai *et al.* [2021\)](#page-10-12). At higher *Ra*, these deviations are evident across all three regions (Zhou *et al.* [2010,](#page-11-1) [2011;](#page-11-2) Scheel, Kim & White [2012;](#page-10-13) Shi, Emran & Schumacher [2012;](#page-10-14) Stevens *et al.* [2012;](#page-10-15) Wang, He & Tong [2016;](#page-10-16) Wang *et al.* [2018\)](#page-10-17). Although dynamic rescaling (Zhou & Xia [2010\)](#page-11-3) improves the agreement in the shear and impact region, significant deviations persist, especially in the ejection region (Pandey [2021\)](#page-10-9).

At low Prandtl numbers, thermal diffusion dominates over viscous effects, leading to different BL dynamics compared with higher-*Pr* fluids. The thermal BL thickness in low-*Pr* fluids exceeds that of the viscous BL, exposing it to direct interaction with the turbulent flow. Previous studies, including those by Scheel & Schumacher [\(2016\)](#page-10-18), Schumacher *et al.* [\(2016\)](#page-10-7), Scheel & Schumacher [\(2017\)](#page-10-8) and Pandey [\(2021\)](#page-10-9), extensively explored these dynamics through numerical investigations. Scheel & Schumacher [\(2017\)](#page-10-8) conducted high-resolution direct numerical simulations at *Pr* values of 0.005 and 0.021, focusing on statistical quantities such as energy dissipation rates and BL thickness scales. They found that the critical *Ra* for transitioning to fully turbulent BLs decreases as *Pr* decreases. The numerical results by Scheel & Schumacher [\(2017\)](#page-10-8) and Pandey [\(2021\)](#page-10-9) suggest that BLs in low-*Pr* convection remain transitional rather than fully turbulent within a Rayleigh number range $Ra \leq 10^{10}$, although increasing fluctuations are observed with increasing *Ra*.

While numerical simulations enable valuable insights, experimental investigations provide empirical evidence and are crucial for validating computational models. So far, the study by Naert, Segawa & Sano [\(1997\)](#page-9-5) is the only one we are aware of that experimentally measures the BL thickness in liquid metal convection. The authors used a movable thermocouple to determine the temperature profile in mercury at the centre of the top plate and examined different approaches for determining the BL thickness. Here, our study aims to experimentally investigate thermal BL dynamics in turbulent liquid metal RBC and provides the first experimental data comparing the thermal BL characteristics both inside and outside the shear-dominated region. We analyse temperature profiles, fluctuation statistics and scaling behaviour, and compare our experimental findings with existing numerical studies.

2. Thermal BL dynamics in liquid metal convection

2.1. *Local vertical temperature gradient in two distinct regions*

The experimental set-up has been thoroughly described in our previous work (Schindler *et al.* [2022\)](#page-10-19). The cylindrical cell has an aspect ratio Γ of 0.5, with dimensions $D =$ 320 mm and $H = 640$ mm. Two copper plates on the upper and lower sides are in contact with the eutectic alloy GaInSn, enabling the investigation of very low *Pr* values ranging from 0.026 to 0.033. The variation in *Pr* arises from the temperature sensitivity of both ν and κ , which comes into play as the mean bulk temperature in the convection cell changes with *Ra*. Our specific focus here lies in analysing the thermal BL structure near the top cold plate. [Figure 1\(](#page-3-0)*a*) shows the sensor arrangement configured for that purpose. Two ultrasonic Doppler velocimetry (UDV) sensors are positioned at a distance of 0.016*H* from the top plate to measure the horizontal velocity of the LSC, *ulsc*, at their cross-section. For measurements of the thermal gradient in the fluid near the top plate, two thermocouple arrays are embedded in the top plate at distances of 0.02*D* and 0.33*D* away from the centre. Each of these arrays contains 10 individual thermocouples, their exact vertical positions are shown in [figures 1\(](#page-3-0)*c*) and [1\(](#page-3-0)*d*).

Examples of the temperature data obtained from these two arrays at $Ra = 3.7 \times 10^8$ are depicted as probability density functions (PDFs) in figures $1(c)$ $1(c)$ and $1(d)$, respectively. Here, we use the normalised temperature defined as $\Theta = (T - T_{cold})/(T_{bulk} - T_{cold})$, where T_{cold} denotes the top plate temperature, and T_{bulk} is the mean bulk temperature obtained by averaging the temperatures of the top and bottom plates, $T_{bulk} = (T_{cold} + T_{cold})$ *Thot*)/2. Three distinct zones can be identified in the temperature profiles measured at the centre (figure $1c$): within the thermal BL, at the edge of the thermal BL and outside of the BL. The PDFs near the plate are narrow and feature temperatures lower than those of the ambient fluid, confirming their location within the thermal BL. The temperature distributions exhibit an almost Gaussian shape in this area, which means there is only a minimal influence from the bulk flow. It is interesting to note the presence of negative values of Θ in this zone, indicating that the values measured by the thermocouple arrays are sometimes lower than *Tcold*. This occurs because the thermal boundary conditions are generally not ideal in liquid metal convection experiments, even when using copper heat exchanger plates. At some point, the heat conduction in the copper plates can no longer compensate for the temperature fluctuations in the fluid quickly enough. For example, Horanyi, Krebs & Müller [\(1999\)](#page-9-6) observed large-scale temperature fluctuations in liquid sodium, which they attributed to an interplay between convective heat transport in the sodium and the conductive equalisation of temperature fluctuations in the adjacent copper plates. Moving to the next zone above this area, the PDFs appear significantly wider and thus suggest an area at the edge of the thermal BL in which the shear flow along the plate is already gaining influence. Finally, we identify a mixing zone, where the measured temperature data are distributed around a constant background temperature at $\Theta = 1$. The skewness in the PDFs observed in this zone is likely attributed to the presence of large-scale thermal plumes and associated turbulent mixing, which cause significant temperature fluctuations and lead to asymmetry in the temperature distributions.

[Figure 1\(](#page-3-0)*d*) illustrates that the temperature PDFs recorded by the second thermocouple array near the side wall show only minor variations with respect to their maximal values and appear flatter and broader compared with the centre region. This can be interpreted

Figure 1. (*a*) Schematic of the experimental set-up with thermocouple arrays and UDV sensors. (*b*) Probability distribution of the LSC direction along the top plate for $Ra = 3.7 \times 10^8$, and probability distribution of temperature data from thermocouple arrays for the same *Ra*, at the centre of the plate (*c*) and near the side wall (*d*).

as an initial indication that the flow influence and related fluctuations in the thermal BL are becoming stronger when the measuring position changes from the centre towards the side wall. While it is evident that the centre of the plate corresponds to the shear-dominated region, the dominance of the LSC-induced shear flow parallel to the copper plate decreases towards the periphery where effects due to plume impact and ejection at the top plate also come into play.

The UDV sensors are used to determine the LSC direction along the top plate according to the procedure suggested by Zürner *et al.* [\(2019\)](#page-11-4). [Figure 1\(](#page-3-0)*b*) presents an exemplary PDF for $Ra = 3.7 \times 10^8$. Here, the location of the thermocouple array near the side wall is aligned with 0° . Highly turbulent and transient LSC structures with constant changes in flow direction along the plates were observed by flow measurements in the same set-up (Wondrak *et al.* [2023\)](#page-10-20). Nevertheless, one or two preferred directions often emerge (for example, here at 75◦ and 285◦), but these vary from experiment to experiment and are therefore difficult to predict. This means that, at different times, our off-centre thermocouple array can be located either upstream (in the impact region) or downstream (in the ejection region) of the LSC, or even to the side of the LSC plane.

Figure 2. Temperature fluctuation profile in the centre (*a*) and near-wall (*b*) regions. Vertical lines with corresponding colours represent the mean thermal BL thicknesses, *H*/(2*Nu*). (*c*) Maximum value of temperature fluctuations normalised by ΔT as a function of Ra.

2.2. *Statistics of the temperature profiles*

For both thermocouple arrays, we compute the root mean square value of the temperature fluctuations which is defined as $\sigma_T(z) = \langle (T - \langle T \rangle)^2 \rangle^{1/2}$, where $\langle \rangle$ indicates time-averaging, and normalise it by the temperature difference between the lower and upper plates $\langle \Delta T \rangle$. These root-mean-square values would be negligible in a laminar BL (Wang *et al.* [2018\)](#page-10-17), but our data in [figure 2](#page-4-0) suggest that the BL is not entirely laminar. According to previous studies (Zhou & Xia [2013;](#page-11-0) Scheel & Schumacher [2016;](#page-10-18) Pandey [2021\)](#page-10-9) temperature fluctuations are smallest within the thermal BL, reach their maximum at the edge of the BL, and decline in the bulk region. The location of σ*T*,*max* can be considered as the position at the edge of the thermal BL where the characteristic temperature profile meets the ambient fluid. For both measuring positions at the centre and the near-wall region, figures $2(a)$ $2(a)$ and $2(b)$ show $\sigma_{T,max}$ occurring close to the mean thermal BL thickness, defined as *H*/(2*Nu*) (Ahlers *et al.* [2009;](#page-9-1) Shishkina & Thess [2009;](#page-10-21) Chillà & Schumacher [2012\)](#page-9-2). A reduction in the BL thickness with increasing *Ra* is reflected by the reduction in the distance between $\sigma_{T,max}$ and the top plate at $z = 0$. At the highest *Ra* considered here, σ*T*,*max* appears to be closer to the plate in the near-wall region than in the centre, whereas the locations of the $\sigma_{T,max}$ are similar in both regions for lower *Ra*. This rough observation does not seem to be consistent with the results of Pandey [\(2021\)](#page-10-9), who found a significant thickening of the BL thickness in the ejection zone. However, Pandey [\(2021\)](#page-10-9) was able to focus his evaluation on the ejection area by moving the measurement points along with the changing LSC plane. We do not have this possibility in the experiment, so we detect a temporal mixture of plume ejection, plume impact and situations in which we measure outside the LSC plane. Pandey [\(2021\)](#page-10-9) also observed a clear decreasing trend of the BL thickness in the ejection region for increasing *Ra*.

In [figure 2\(](#page-4-0)*c*), we plot the normalised values $\sigma_{T,max}$ as a function of *Ra*. The exponent of the slope is $Ra^{-0.102}$ for the centre region and $Ra^{-0.120}$ for the side wall region. Especially in the side wall region, this scaling is similar to the recently reported value of −0.118 (Samuel *et al.* [2024\)](#page-10-22), even though their value derives from spatial averaging and their configuration (Cartesian domain with $\Gamma = 4$) differs from that considered in this study. However, previous experimental studies with $\Gamma = 0.5$ (Castaing *et al.* [1989;](#page-9-7) Wu & Libchaber [1992;](#page-10-23) Niemela *et al.* [2000\)](#page-9-8) have reported steeper exponents for the central region, approximately −0.144 to −0.147, indicating a stronger dependence on *Ra*. Additionally, Samuel *et al.* [\(2024\)](#page-10-22) found that the exponent can vary depending on the

Figure 3. Dimensionless mean temperature profiles as functions of $z/\delta_T(x, t)$ in the centre (*a*) and near-wall (*b*) regions. (*c*) Shape factor *S* as a function of *Ra*. The horizontal line denotes the shape factors for the Prandtl–Blasius case (*S* ∼ 2.47 for 0.026 ≤ *Pr* ≤ 0.033).

spatial range considered, with their values changing to -0.140 in the bulk region. Here, we focus solely on the maximum temperature fluctuation values near the plate.

The decline in $\sigma_{T,max}/\Delta T$ is explained by Pandey [\(2021\)](#page-10-9) with the argument that, with increasing *Ra*, the temperature difference between the plate and the ambient fluid at the edge of the BL decreases which is confirmed by our temperature profiles presented in [figure 3\(](#page-5-0)*b*). This should also reduce the temperature difference between the bulk fluid and the plumes that are formed. Correspondingly, the decrease of $\sigma_{T,max}$ is particularly pronounced at the off-centre position, as plume ejection events are expected to occur only near the side wall, not at the centre. Moreover, figure $2(c)$ shows that $\sigma_{T,max}$ is larger in the near-wall region compared with the centre region across the entire range of *Ra* examined here. This is to be expected, as the influence of the shear flow decreases the further away the observation point is from the centre of the plate. Large-scale velocity fluctuations associated with plume impact or ejection are becoming more relevant near the side wall. Due to the small *Pr*, this is directly reflected in the behaviour of the thermal BL, indicating a starting mixing between the BL and the turbulent bulk flow. In contrast, in the shear-dominated region, where no significant velocity components normal to the plate surface occur, there is less exchange between thermal BL and bulk flow.

The averaged temperature profiles beneath the top plate are plotted in [figures 3\(](#page-5-0)*a*) and [3\(](#page-5-0)*b*). Many previous studies have shown that dynamically rescaled profiles can provide an intuitive comparison with the PBP profile (Zhou *et al.* [2011;](#page-11-2) Scheel *et al.* [2012;](#page-10-13) Shi *et al.* [2012;](#page-10-14) Stevens *et al.* [2012;](#page-10-15) Wang *et al.* [2016,](#page-10-16) [2018\)](#page-10-17). A time-averaged temperature profile in a fixed reference frame as a function of the height *z* contains mixed dynamics with contributions from inside and outside the BL range, as the BL thickness is constantly changing during the measurement. To achieve a clear separation of those dynamics, Zhou & Xia [\(2010\)](#page-11-3) studied BL quantities within a time-dependent frame that varied with the instantaneous BL thickness. The rescaled vertical distances and the averaged temperature profiles in the dynamic frame are defined as

$$
\xi^*(t) = z/\delta_T(x, t),\tag{2.1}
$$

$$
\Theta^*(\xi^*) = \langle \Theta(z,t)|_{z=\xi^*(t)\delta_T(x,t)} \rangle.
$$
 (2.2)

Here, the instantaneous local thermal BL $\delta_T(x, t)$ is obtained using the slope method (Zhou *et al.* [2011;](#page-11-2) Scheel *et al.* [2012;](#page-10-13) Wagner *et al.* [2012\)](#page-10-4), where $\delta_T(x, t)$ is the distance from the plate to an intersection point where the line with the slope of the temperature profile directly at the plate meets the bulk temperature. Here, $\sigma_{T,max}$ is used to specify the number of data points used for calculating the temperature slope within the BL

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 $(0 \le z \le z(\sigma_{T,max}))$. The number of selected sensors depends on *Ra* since the position of σ*T*,*max* varies with *Ra*, but this number for a given *Ra* remains fixed over time.

Previous studies show that the dynamically rescaled temperature profile agrees well with the PBP profile in the impact and shear-dominated regions, indicating a laminar behaviour of the BL in these regions (Zhou & Xia [2010;](#page-11-3) van der Poel *et al.* [2015;](#page-10-6) Pandey [2021\)](#page-10-9). In contrast, the profile deviates significantly from the PBP profile in the ejection region due to stronger turbulent fluctuations. Consistent with these previous studies, our measurements in the shear-dominated region demonstrate a very good agreement with the PBP profile for all *Ra* (see [figure 3](#page-5-0)*a*), whereas significant deviations from the PBP profile are observed for the off-centre position (see [figure 3](#page-5-0)*b*). Here, the difference to the PBP profile increases with growing *Ra*, indicating an increase in disturbances impairing the laminar character of the BL.

To quantitatively investigate the deviation of the temperature profile from the PBP profile, we calculate the shape factor *S*∗ from the temperature profile in the dynamic frame, which is defined as (Scheel *et al.* [2012;](#page-10-13) Scheel & Schumacher [2017;](#page-10-8) Pandey [2021\)](#page-10-9)

$$
\delta_d^* = \int_0^\infty \left(1 - \frac{\Theta^*}{\Theta_{max}^*}\right) \mathrm{d}\xi^*,\tag{2.3}
$$

$$
\delta_m^* = \int_0^\infty \left(1 - \frac{\Theta^*}{\Theta_{max}^*}\right) \frac{\Theta^*}{\Theta_{max}^*} \, \mathrm{d}\xi^*,\tag{2.4}
$$

$$
S^* = \delta_d^* / \delta_m^*.
$$
 (2.5)

Here, δ_d^* and δ_m^* represent the displacement and momentum thicknesses of the profiles after being rescaled by the dynamic frame. In figure $3(c)$, the black line denotes the shape factor for the PBP profile, $S \sim 2.47$ in the range $0.026 \le Pr \le 0.033$. We observe that *S*[∗] is smaller than 2.47 for almost all of our measurements. The difference between the dynamically rescaled temperature profiles and the PBP profile increases with increasing *Ra*. This is because the BL becomes thinner and more strongly influenced by turbulence, which means that the profile reaches its asymptotic value more slowly (Pandey [2021\)](#page-10-9). Larger deviations are found in the region near the side wall, which is more affected by turbulent fluctuations of the flow. The results in [figure 3\(](#page-5-0)*c*) demonstrate that the local thermal BLs are not fully laminar whereby the nature of the BL becomes increasingly transient with growing *Ra*.

2.3. *Scaling of BL thickness with Ra*

[Figure 4](#page-7-0) presents the thickness of both the mean thermal and viscous BLs as a function of *Ra*. The local instantaneous thermal BL $\delta_T(x, t)$ is determined using the slope method, as described in § [2.2.](#page-4-1) From these data, we then compute the time-averaged value for each *Ra*, denoted as $\delta T = \langle \delta T(x, t) \rangle$. The continuous reduction of the mean thickness of the thermal BL, δ_T , with increasing Ra , is evident for both the shear-dominated region at the plate centre and the position near the side wall. Moreover, the width of the thermal BL is larger near the side wall. The thermal BL thickness is inversely proportional to the vertical diffusive heat flux at the plate, which obviously increases with *Ra* and is lower near the sidewall than in the shear-dominated region. It has also been reported in previous studies (Wagner *et al.* [2012;](#page-10-4) Scheel & Schumacher [2014;](#page-10-5) Pandey [2021\)](#page-10-9) that the variation of the BL width aligns with the direction of the LSC along the plate, in particular, the BL thickness increases in the downstream direction from the plate centre.

We observe different scaling exponents for the two measuring positions under consideration here. While δ_T shows a $Ra^{-0.20}$ scaling at the centre region (in accordance

Figure 4. Time-averaged thermal and viscous BL thicknesses as a function of *Ra*.

with Naert *et al.* [1997\)](#page-9-5), it scales like *Ra*−0.²⁶ near the side wall. The same value of [−]0.26 has been reported by Scheel & Schumacher [\(2016\)](#page-10-18) for δ_T averaged over the plate area. Pandey [\(2021\)](#page-10-9) obtained an exponent of -0.25 , also for a horizontally averaged value of δ_T . In view of the aspect that the shear-dominated zone probably only occupies a small part of the total area of the plate, this result is understandable. In our case, the different exponents also mean that the difference in BL thickness between the centre and the side wall region is greatest at low *Ra*, whereas the thicknesses are similar at high *Ra*. This observation is consistent with the findings of Pandey [\(2021\)](#page-10-9), who observed a much steeper decline of δ_T in the ejection region as compared with the shear-domination zone.

Another parameter for characterising BL behaviour is the displacement thickness (Schlichting & Gersten [2016\)](#page-10-24). It provides a measure of the effective thickness of the thermal BL and is defined in a fixed frame as Scheel & Schumacher [\(2017\)](#page-10-8)

$$
\delta_{T,dis} = \int_0^\infty \left(1 - \frac{\bar{T}}{\bar{T}_{bulk}}\right) dz.
$$
 (2.6)

Scheel & Schumacher (2017) suggest that the displacement thickness scales with *Ra*^{−0.25} for a laminar BL, whereas it decreases with an exponent of −0.1 for a turbulent BL. It is shown in [figure 4](#page-7-0) that $\delta_{T,dis}$ decreases with an exponent of -0.26 for both measuring positions. This analysis indicates that our thermal BLs are still in a transitional state and therefore exhibit laminar-like scaling rather than turbulence-like scaling.

[Figure 4](#page-7-0) also contains the viscous BL thickness, δ_v , for comparison. However, this variable is not directly accessible for direct measurements in our current experimental set-up. Instead, we employ the equation for the Blasius BL thickness (Schlichting $\&$ Gersten [2016\)](#page-10-24), defined as $\delta_v = aH/\sqrt{Re_H}$, under the assumption that the viscous BL remains in the laminar regime. Here, the height *H* is used as the characteristic length for Reynolds number, $Re_H = u_{LSC}H/\nu$. The characteristic LSC velocity, u_{LSC} , is measured as the time-averaged horizontal velocity beneath the top plate by means of the UDV sensors shown in [figure 1\(](#page-3-0)*a*) (see also Zürner *et al.* [2019\)](#page-11-4). To determine δ_{v} and the appropriate coefficient *a*, we adopt the assumption that the ratio of the thermal BL to the viscous BL remains constant for a given *Ra*. Shishkina *et al.* [\(2010\)](#page-10-25) derived the following relationship between the thermal BL and the viscous BL for $3 \times 10^{-4} \le Pr < 3$:

$$
\delta_T / \delta_v \sim Pr^{-0.357 + 0.022 \log Pr}.
$$
 (2.7)

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Since u_{LSC} is measured at the intersection of the two UDV measuring lines at the centre of the top plate (see [figure 1](#page-3-0)*a*), we input the δ_T data from the centre position into [\(2.7\)](#page-7-1). The resulting coefficient was found to be *a* ∼ 0.53, which is similar to values reported in previous studies: $a = 0.482$ by Grossmann & Lohse [\(2002\)](#page-9-9) and $a = 0.6$ by Zhou & Xia [\(2010\)](#page-11-3). The δ_{ν} data presented in [figure 4](#page-7-0) decrease with a scaling of $Ra^{-0.22}$. This scaling is consistent with $\overline{Re} \sim Ra^{0.45}$, which has been identified in many previous studies (Qiu & Tong [2001;](#page-10-26) Grossmann & Lohse [2002;](#page-9-9) Ahlers *et al.* [2009;](#page-9-1) Scheel & Schumacher [2017;](#page-10-8) Schindler *et al.* [2022;](#page-10-19) Xu, Zhang & Xia [2022\)](#page-10-27). Consequently, this leads to a *Ra* dependence of $\delta_v \sim Re^{-0.5} \sim Ra^{-0.225}$ in the laminar regime (Shi *et al.* [2012\)](#page-10-14), a value similar to our observed scaling of −0.22. Thus, the authors suggest that, given the limitations of the velocity measurements in the current set-up, the observed scaling of $\delta_v \sim Ra^{-0.22}$ is consistent with a laminar BL.

3. Summary and conclusions

The present experimental study is dedicated to the investigation of the thermal BL in turbulent liquid metal RBC, within the *Pr* range of 0.026 to 0.033 and *Ra* up to 2.9 \times 10⁹. For this purpose, we measure vertical temperature profiles at two positions directly below the top plate. One of the measuring positions is in the centre area of the plate, over which the LSC constantly flows so that a shear-dominated zone can be certainly assumed here. The second thermocouple is installed at a radial distance of 0.33*D* from the centre of the plate. It is well known that the horizontal velocity component of the LSC weakens with increasing distance from the plate centre. In the lateral areas, thermal plumes either form and detach (plume ejection) or impinge (plume impact) when they come from the opposite plate.

Our analysis reveals significant differences in temperature profiles, fluctuation statistics, and BL thickness scaling between the two considered measuring positions. In the shear-dominated region, temperature profiles resemble laminar BL profiles (the PBP profile), whereas in the region near the side wall, stronger fluctuations lead to deviations from the laminar behaviour. These discrepancies become more pronounced at higher *Ra* indicating an increasing influence of turbulent fluctuations with increasing *Ra*. In the present study, the viscous BL δ_{ν} , which, in low-*Pr* fluids, is significantly smaller than the thermal BL δ_T , could not be measured directly. However, a rough estimate confirms that the viscous BL can be regarded as laminar under the conditions considered here. The much thicker thermal BL, therefore, extends into the zone of turbulent flow and could therefore be directly affected by it. Our results also show this but do not provide evidence for a transition to a fully turbulent thermal BL.

The thermal BL width, δ_T , shows distinct scalings for the centre and side wall regions, *Ra*^{−0.20} and *Ra*^{−0.26}, respectively. The difference in the BL thickness is most pronounced for small *Ra*, but the different scaling exponents result in almost the same BL thickness for $Ra \approx 10^9$. The thermal displacement thickness $\delta_{T,dis}$ declines with an exponent of −0.26 in both regions which indicates a behaviour akin to a laminar BL. This appears to be contrasted by the deviations of our data from the characteristic value of the shape factor *S*∗ for a PBP profile even after the application of dynamic rescaling. However, only minor deviations occur in the shear-dominated zone, whereas significantly lower values were determined for the side wall region at high *Ra*. The thermal BL profiles deviate from the PBP profile in both regions, with larger discrepancies found in the side wall region where stronger turbulent fluctuations occur frequently. This suggests that a possible departure from the laminar state to a transitional or even turbulent BL is most likely to

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occur first in the side wall region. Growing turbulent fluctuations with increasing *Ra* affect the laminar character of the thermal BL. However, according to the findings in this study, the BL does not yet become fully turbulent but shows a transitional behaviour in the area near the side wall at high *Ra*. The larger local BL width in the side-wall region corresponds to the formation and detachment of coarser plumes resulting in a less steep vertical temperature gradient in the side-wall region compared with the centre region (Pandey [2021\)](#page-10-9) (see [figure 3\)](#page-5-0). It is interesting to note that our experimental findings agree very well with the numerical results of Pandey [\(2021\)](#page-10-9), although due to the volatile nature of the LSC, our measurements at the sidewall represent a time average over the BL behaviour in different areas (ejection, impact, laterally with respect to the LSC plane), whereas the analysis by Pandey [\(2021\)](#page-10-9) fits exactly in the LSC direction. We assume that measurements focusing explicitly on the ejection zone could reveal even more pronounced deviations from a laminar BL. Therefore, in further experiments, we plan to increase the number of temperature measurement points in the near-wall region and combine this with simultaneous velocity measurements to determine the instantaneous LSC direction and localise the ejection zone. The continuation of these experiments will provide valuable insights into the thermal BL dynamics in turbulent liquid metal convection, contributing to a better understanding of the heat transfer mechanism.

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