

# Corrigendum: On the relation of a distributive lattice to its lattice of ideals

Herbert S. Gaskill

There are errors in my paper [1], Lemma 1 and from the end of Lemma 4 to the end of the paper.

LEMMA 1. *If  $L$  is any finite lattice and  $L$  has a point which is both join and meet reducible then  $L$  is not weakly transferable.*

We replace Lemma 5 by the following sequence.

Let  $a \in L$  be fixed of maximal height such that  $\sum(J_a\psi) < \prod(M_a\psi)$ .

LEMMA 5. *If  $H = \{x : x \not\leq a\}$ , then*

$$\sum(J_a\psi) + \prod(H\psi) = \prod(M_a\psi).$$

Let  $J(L)$  be the collection of join irreducibles of  $L$ .

LEMMA 6. *There is a  $\psi'_1 : J(L) \rightarrow L^*$  such that:*

- (1)  $\psi'_1$  is order preserving;
- (2)  $x\psi \leq x\psi'_1 \in x\phi$ ;
- (3) if  $x \leq a$ , then  $x\psi'_1 \leq a\psi$ ;
- (4) if  $z \not\leq a$  and  $x \leq z$ , then  $x\psi'_1 \leq z\psi$ ;
- (5)  $\sum(J_a\psi'_1) = \prod(M_a\psi)$ .

THEOREM 3. *Let  $L$  and  $L^*$  be as before. If  $L$  can be embedded in*

---

Received 24 January 1973.

$T(L^*)$  then  $L$  can be embedded in  $L^*$ .

REMARK. The Theorem follows since Lemmas 5 and 6 allow us to obtain a new meet isomorphism  $\psi_1$  such that

$$\sum (J_a \psi_1) = \prod (M_a \psi_1)$$

Further, this isomorphism has one less failure whose height is that of  $a$  than did  $\psi$ .

### Reference

- [1] Herbert S. Gaskill, "On the relation of a distributive lattice to its lattice of ideals", *Bull. Austral. Math. Soc.* 7 (1972), 377-385.

Department of Mathematics and Astronomy,  
University of Manitoba,  
Winnipeg,  
Manitoba,  
Canada.